

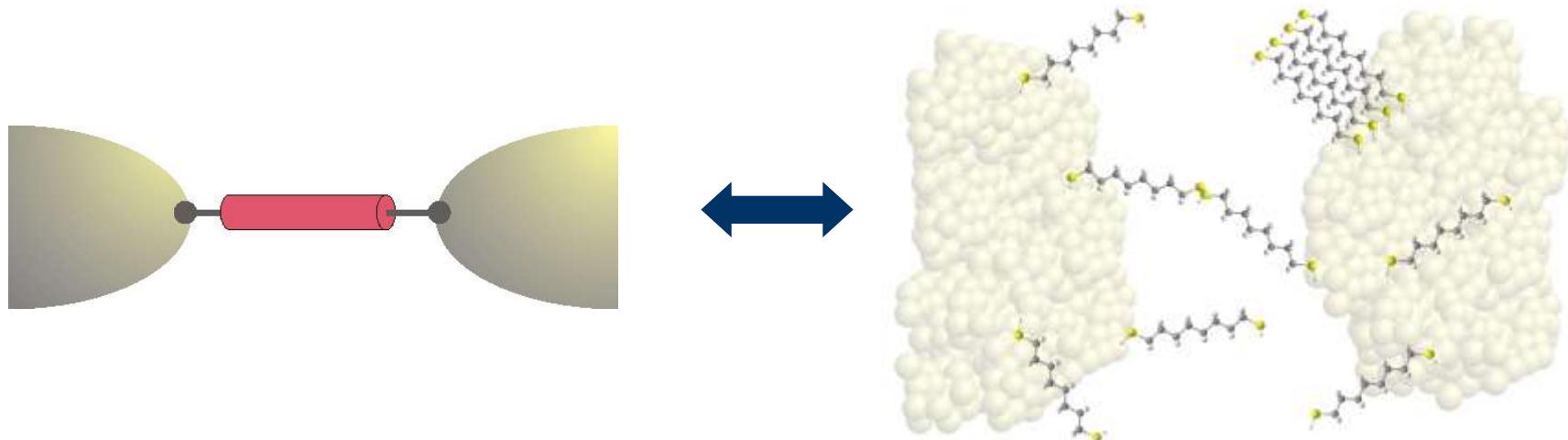
# *Molecular and carbon-based electronic systems*

## *Lecture 6*

## ***Molecular junctions basics II***

## ***& spectroscopy***

# molecular junction



## nanometer and molecular-scale junctions

- structural disorder
- interactions
- fluctuations

*electrodes and junction geometry  
anchoring, self-assembly, polymerization  
mobility of (surface) atoms, molecular distortions,  
multiple local energy minima*

## typ. energies

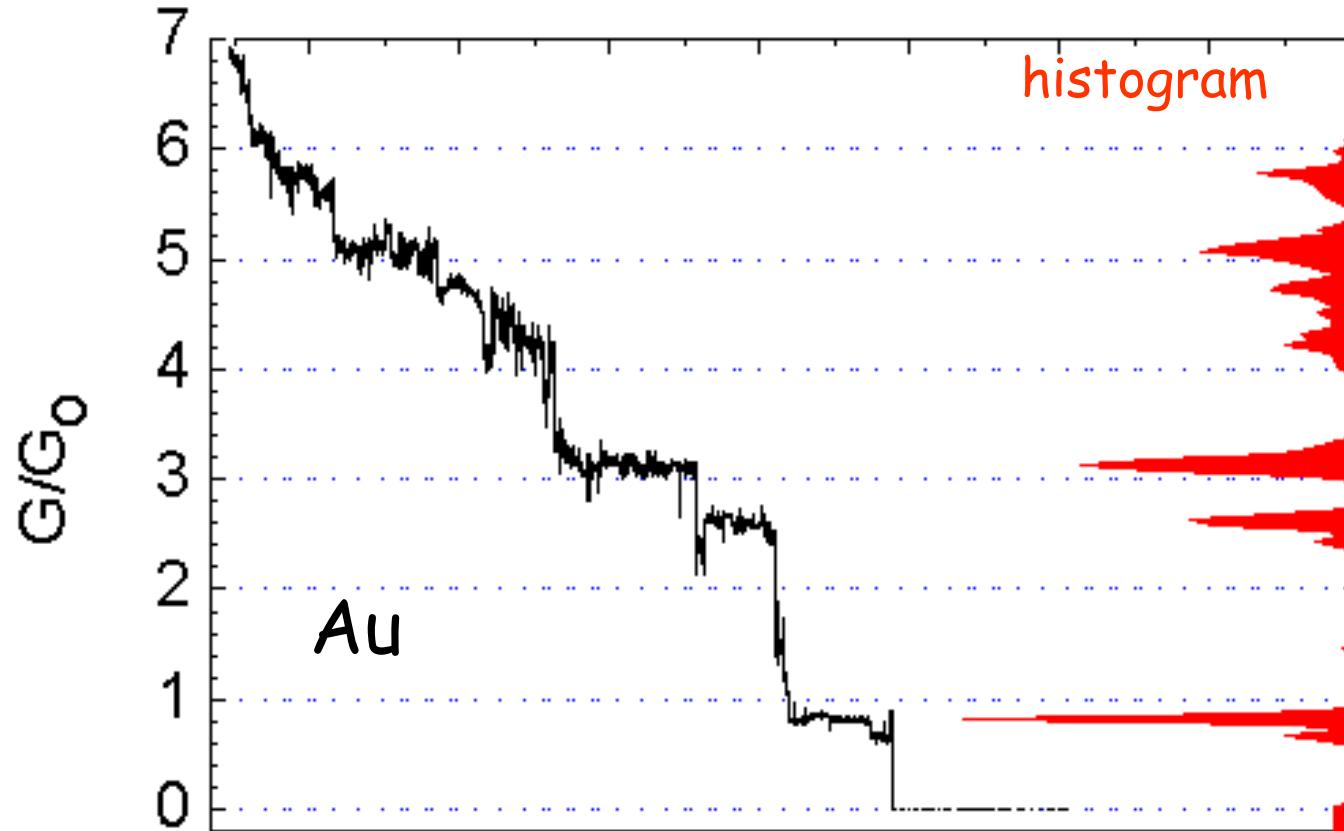
- Au-Au, Au-S bond
- surface Au-Au
- benzene-benzene

0.7-1.5eV *Kawai et al., APL 2008, Tao et al., JACS 2009, JL arrays*  
~ 0.3eV  
~ 0.1eV *Jorgensen et al., JACS, 1990*

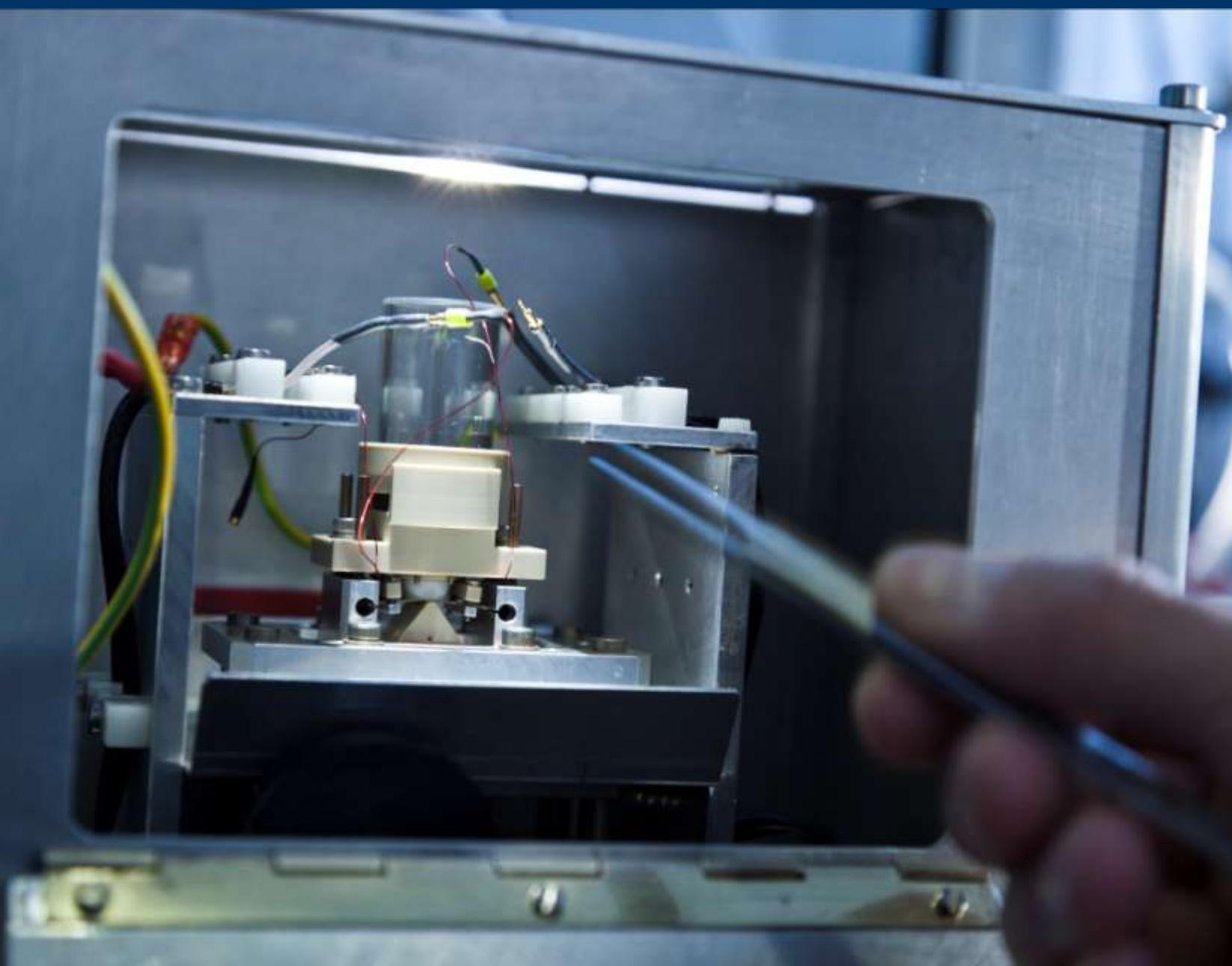
# break junctions

## Conductance quantization for Au contact

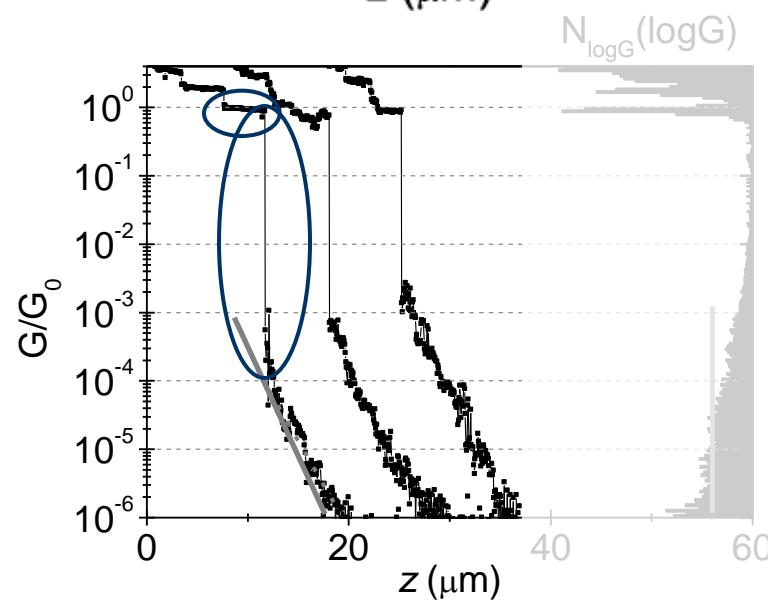
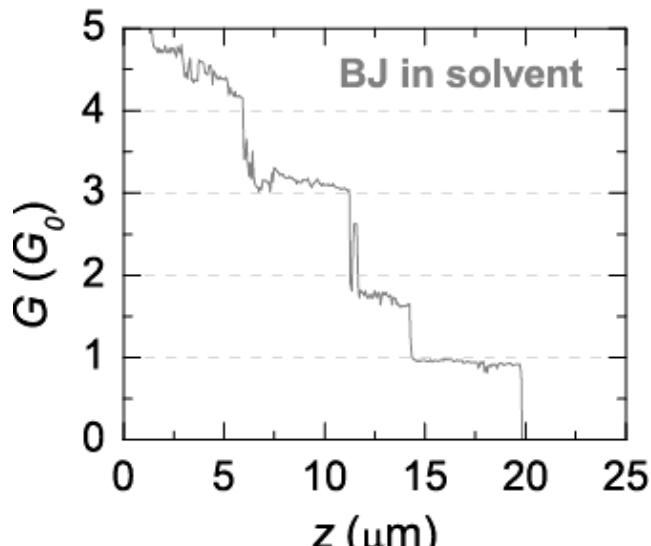
$$n = 1 \text{ with } T = 1 \quad \Rightarrow \quad G = \frac{2e^2}{h} \sum_n T_n = G_0 = \frac{2e^2}{h} = 77.5 \mu\text{S}$$



# break junctions in liquid environment



# opening: conductance vs elongation



**break junction opening**  
(solvent:THF/mesitylene 1:4 v/v)

conductance quantization,  
plateaus

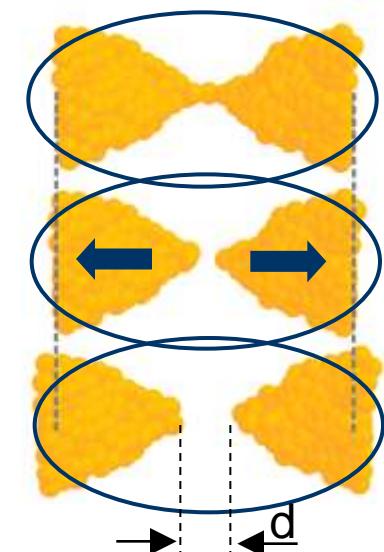
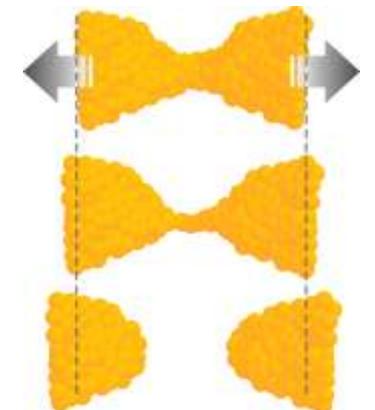
$$G_0 = \frac{2e^2}{h} = 77.5 \mu\text{S}$$

cf e.g. Agrait et al., Phys. Rep. 2003

- last Au G-plateau ( $\sim 1 G_0$ )
- breaking of Au bridge
- tunneling regime

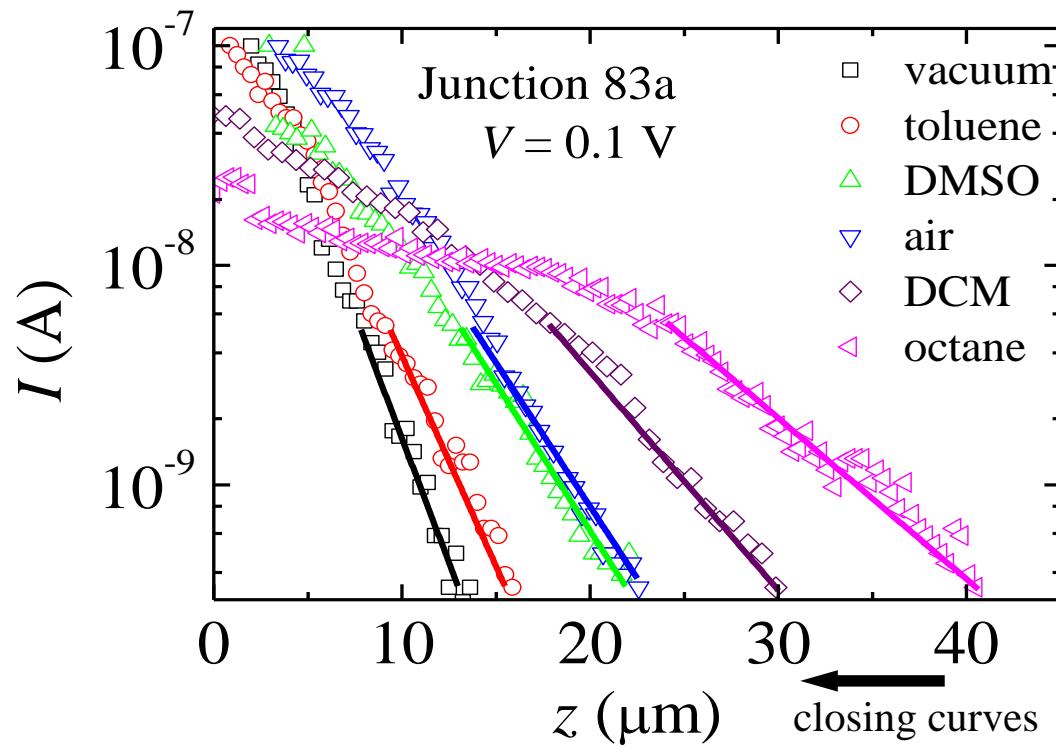
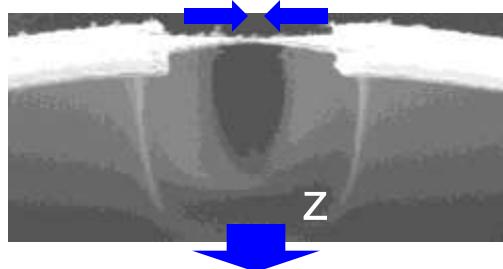
$$G \propto e^{-\beta d}$$

- statistics: histogram  
tunneling background  
 $\Leftrightarrow$  const.

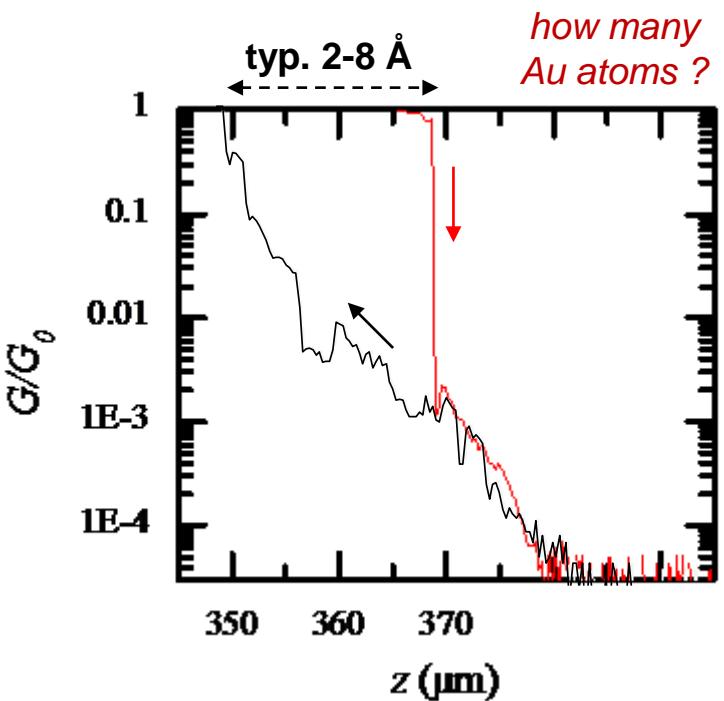


# tunneling regime

gap open,  
close the  
junction



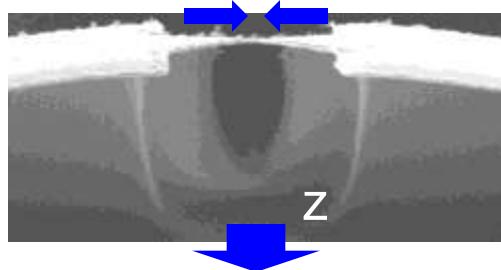
opening-closing trace



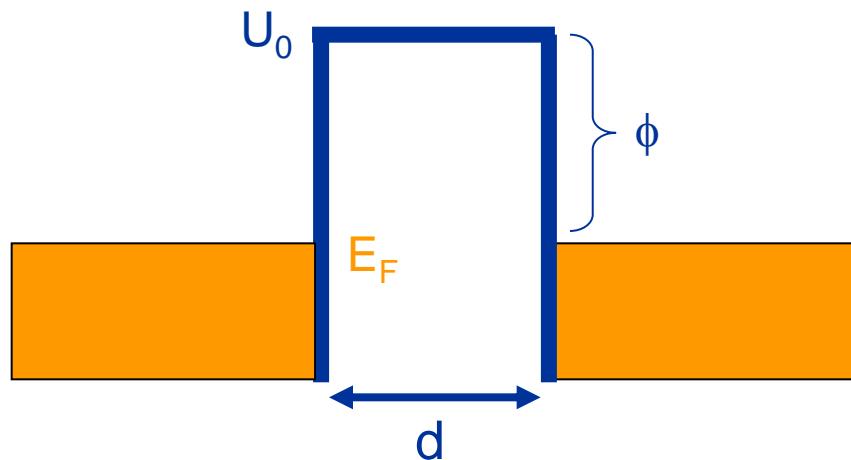
liquid ~ effective medium  
 in first approx.

# tunneling regime

gap open,  
close the  
junction



$$I \propto \exp\left(-\frac{2d}{\hbar} \sqrt{2m\phi}\right)$$



$$d=r \cdot z \quad r = \text{reduction factor}$$

$$B = 2r \sqrt{2m\phi} / \hbar$$

$$\rightarrow I \propto e^{-Bz}$$

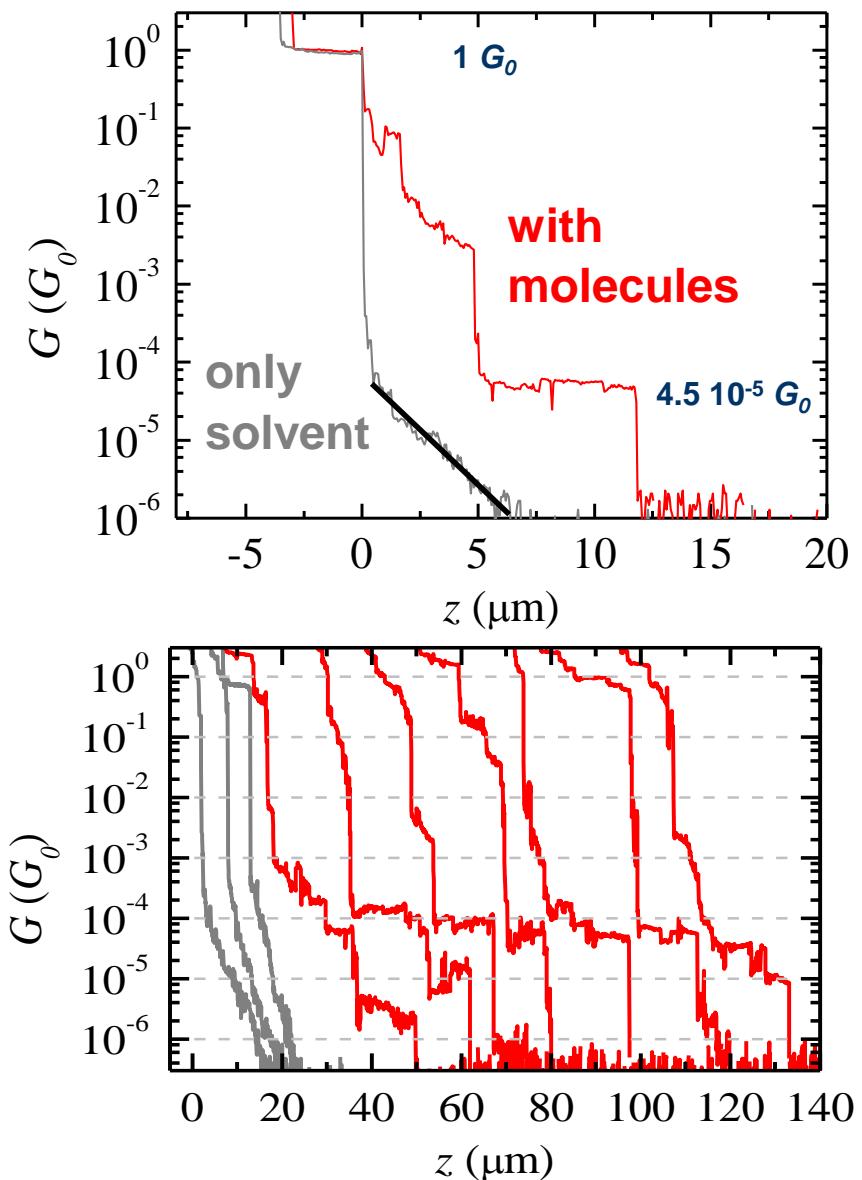
$$\phi = U_0 - E_F$$

in vacuum: metal workfunction

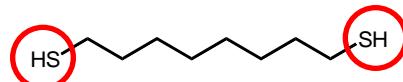
in solvent: apparent barrier height

contacting simple  
molecules

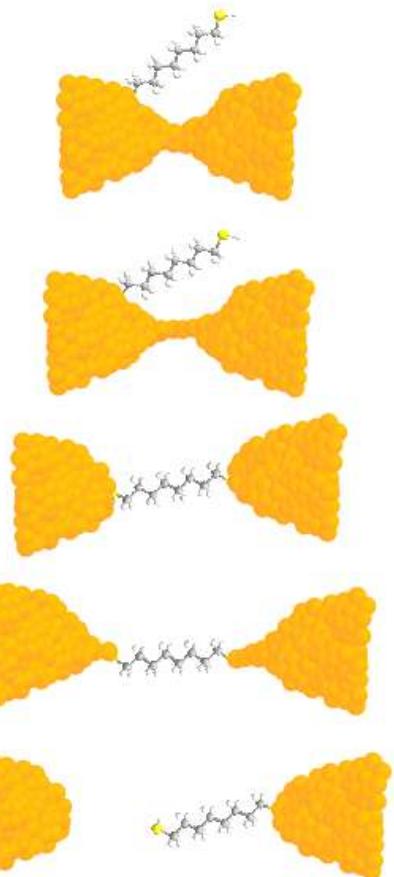
# signature of a molecular junction



**example:**  
*alkanedithiols*



large HOMO-LUMO gap  
(few eV),  $\sim$  no solvent effect

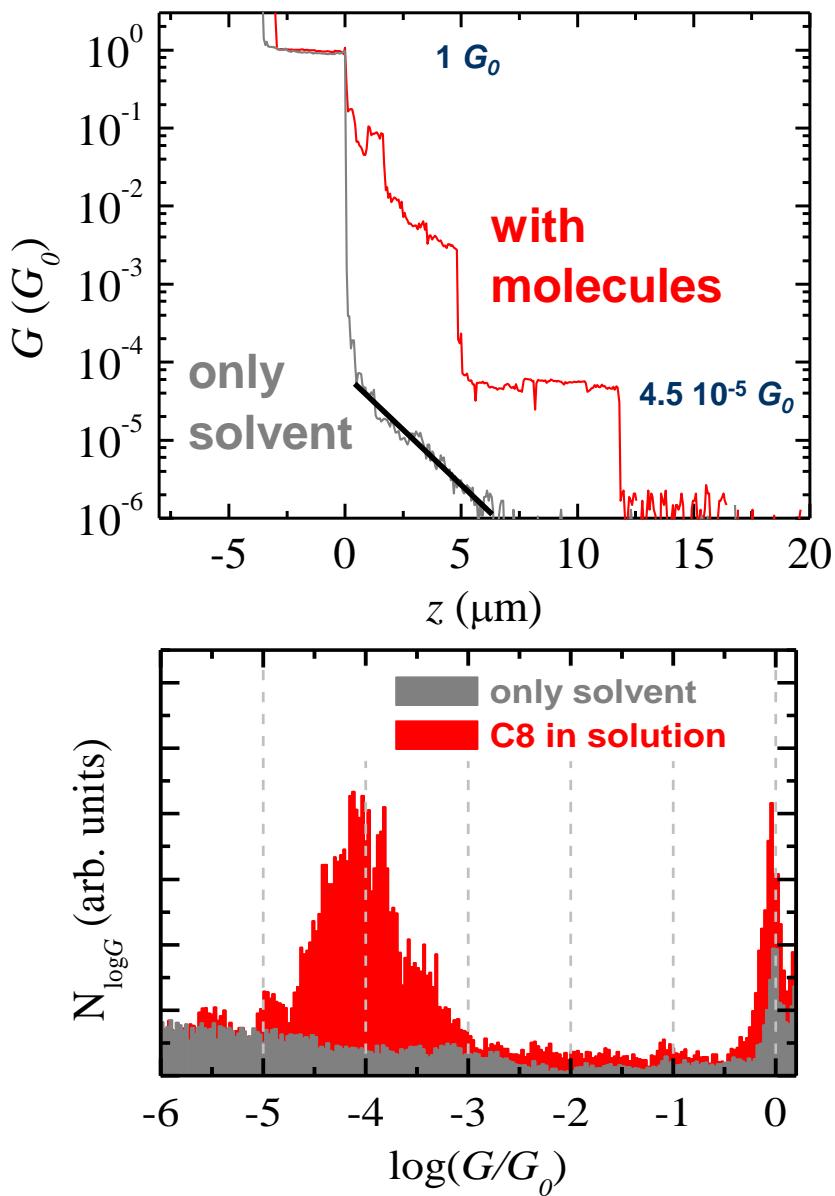


**molecular signature:**  
*plateau (at  $G \ll G_0$ )*

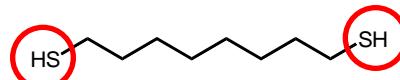
(Reichert et al., PRL 2002, Tao et al., Science, 2003, Nano Lett. 2004, JACS 2007)

only solvent: Mesitylene  
with molecules: 0.1 M octanedithiol in Mesitylene

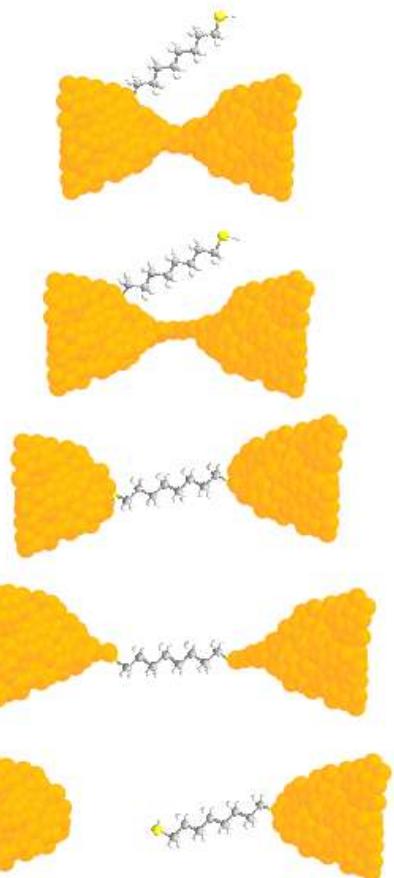
# signature of a molecular junction



**model system:  
alkanedithiols**



large HOMO-LUMO gap  
(few eV), ~no solvent effect



**molecular signature:  
plateau (at  $G \ll G_0$ )  
↔ peak in (log-G)  
histogram**

- *plateau in 20-60% curves*
- *conductance window > 6 orders of mag.*

understanding transport  
through molecules

# Landauer approach to electron transport

Electronic transport as scattering problem

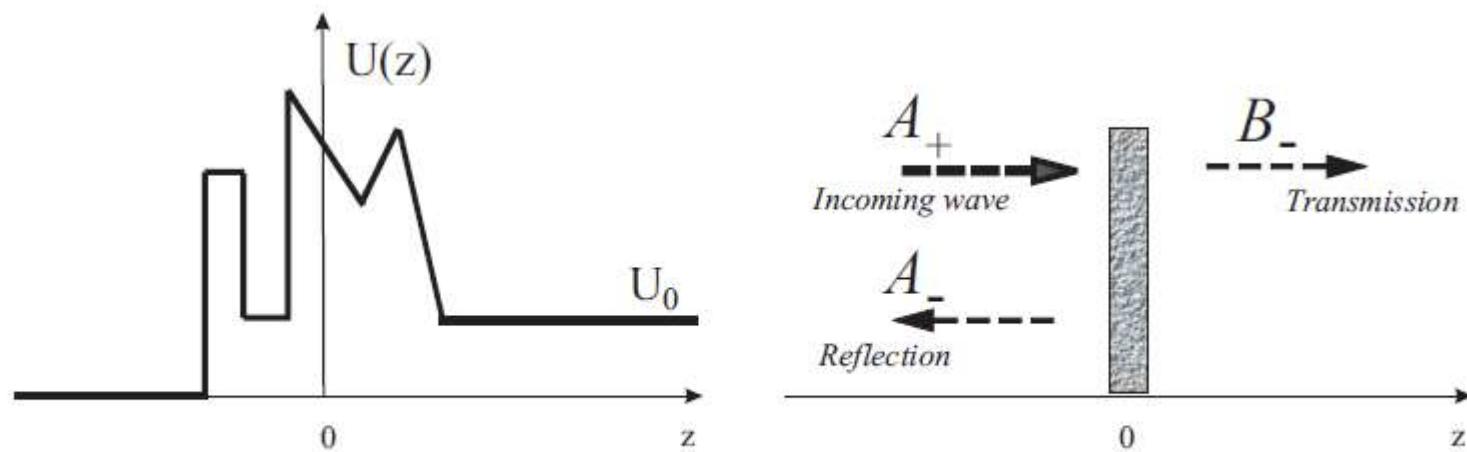
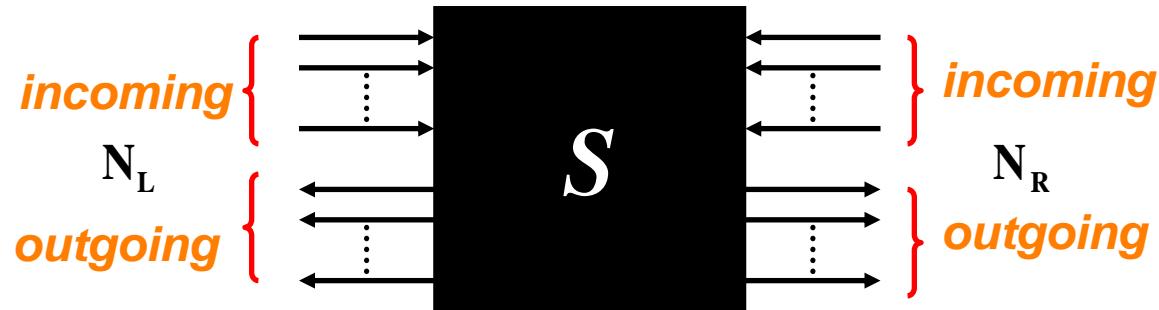
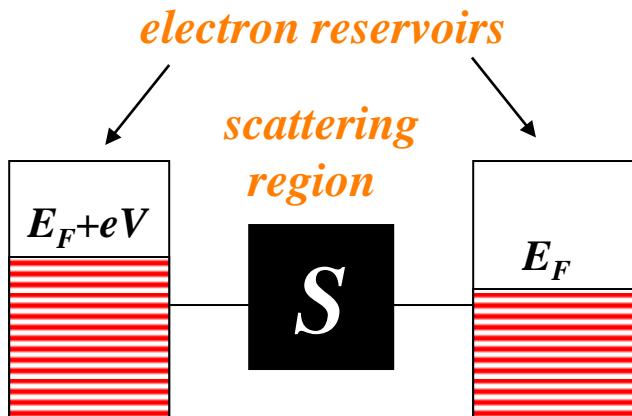
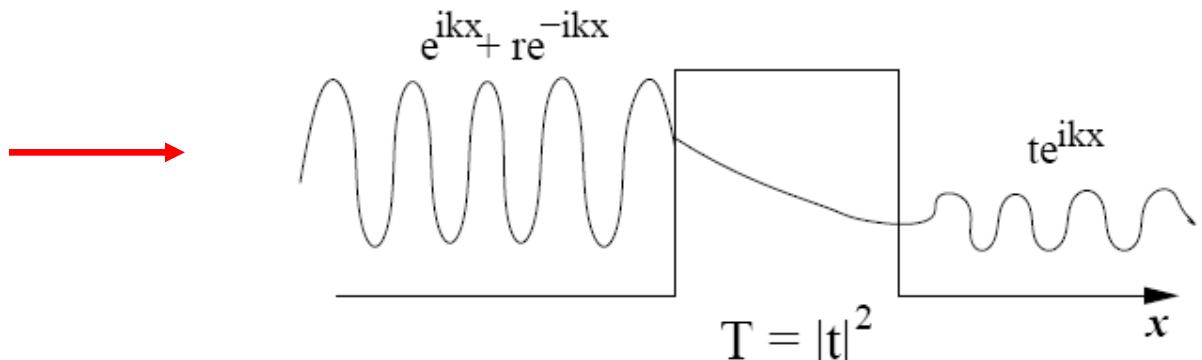


Fig. 1.2. One-dimensional potential. Reflection and transmission.

# Landauer approach to electron transport

Electronic transport as scattering problem



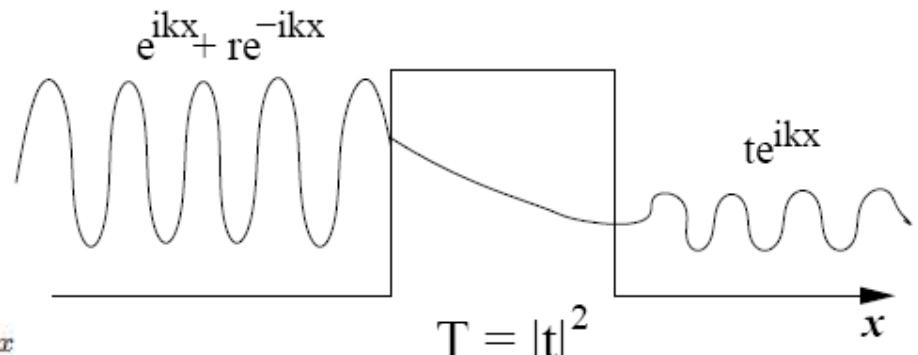
$$G = \frac{2e^2}{h} T(E_F)$$

$G$  = conductance

$T(E_F)$  = transmission at the Fermi energy

# Landauer approach to electron transport

Electronic transport as scattering problem



one electron approach, phase coherent electrons in reservoir, thermal eq.  
plane waves ( $L$ : lenght of system):  $(1/\sqrt{L})e^{ikx}$

**electrical current density** (calc. on right hand side of scattering potential) carried by one electron

$$J_k = \frac{\hbar}{2mi} \left[ \psi^*(x) \frac{d\psi}{dx} - \psi(x) \frac{d\psi^*}{dx} \right] = \frac{e}{L} v(k) T(k) \quad v(k) = \hbar k / m$$

*group velocity*

**solid state device**: sum over  $k$  (many electrons) and add Fermi distrib. for Left and Right reservoirs

$$J_{L \rightarrow R} = \frac{e}{L} \sum_k v(k) T(k) f_L(k) [1 - f_R(k)]$$

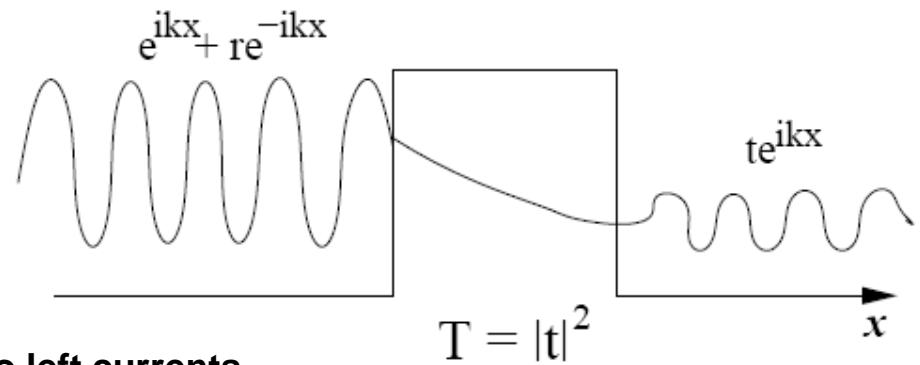
**integrate**  $(1/L) \sum_k g(k) \rightarrow 1/(2\pi) \int g(k) dk$

**variable change**  $dk/dE = (dE/dk)^{-1} = m/(\hbar^2 k)$  using  $E = \hbar^2 k^2 / (2m)$

*conducting electrons: Fermi gas (non-interacting electrons)*

# Landauer approach to electron transport

Electronic transport as scattering problem



hence, we can write the **left to right** and **right to left** currents

**NB:** the transmission probability is the same, no matter in which direction the barrier is crossed

$$J_{L \rightarrow R} = \frac{e}{h} \int dE T(E) f_L(E) [1 - f_R(E)]$$

$$J_{R \rightarrow L} = \frac{e}{h} \int dE T(E) f_R(E) [1 - f_L(E)]$$

total current through junction

*NB: 1D situation: no difference between total current and current density*

$$I(V) = J_{L \rightarrow R} - J_{R \rightarrow L}$$

$$\stackrel{\text{spin}}{\longrightarrow} I(V) = \frac{2e}{h} \int_{-\infty}^{\infty} dE T(E) [f_L(E) - f_R(E)] \quad \text{Landauer}$$

at  $T=0$ , low bias voltages (linear regime)

$$I = GV \quad \text{with} \quad G = (2e^2/h)T \quad G_0 = \frac{2e^2}{h} \quad \text{conductance quantum}$$

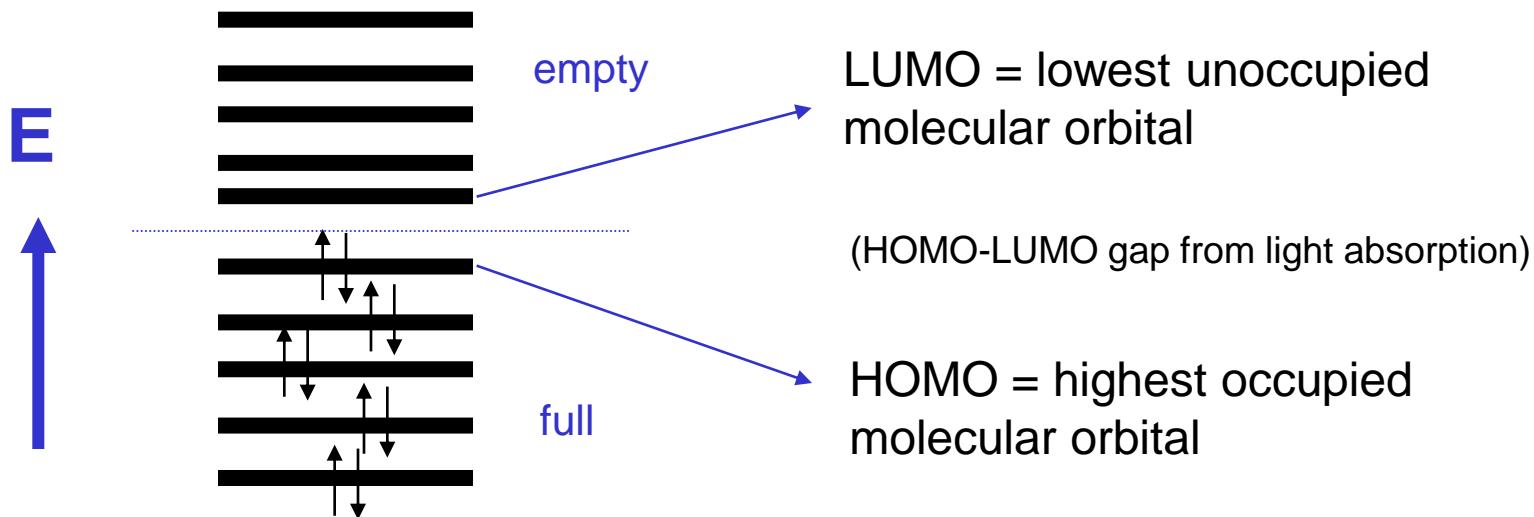
and  $T=T(E_F)$

$$G_0 \simeq (12.9k\Omega)^{-1}$$

# molecular energy levels

## (isolated) molecule

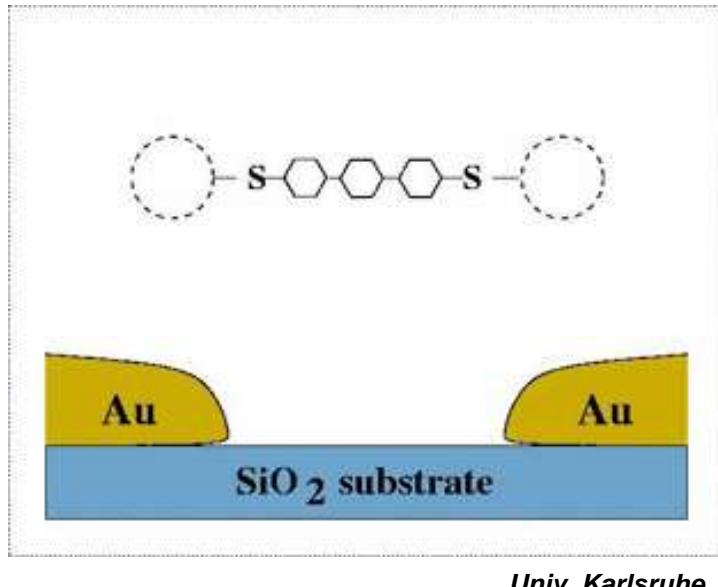
quantum system with spectrum of discrete energy states (molecular orbitals)



⇒ ‘Particle in a box’: molecule is small box

box smaller  $\Leftrightarrow$  levels more spaced ( $\delta E > k_B T$ )

# making contact...

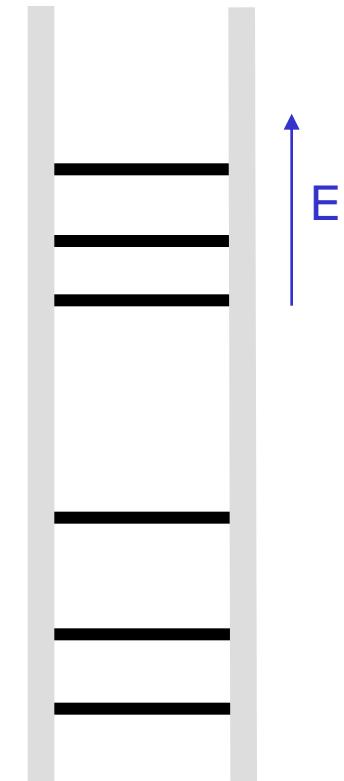


*Univ. Karlsruhe*

⇒ typ. 2 regimes: weak  
or strong coupling

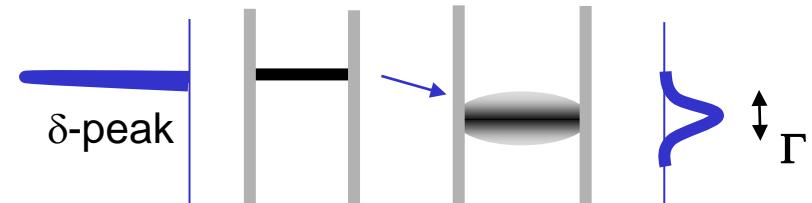
**Au:** many levels: ~ continuous  
**molecule:** few discrete, levels

empty



# "good" contact

energy levels



- **broadening:**  $\Gamma$

delta function

$\Rightarrow$  Lorentzian DOS

$$D(E) = \frac{1}{2\pi} \frac{\Gamma}{(E - E_0)^2 + (\Gamma/2)^2}$$

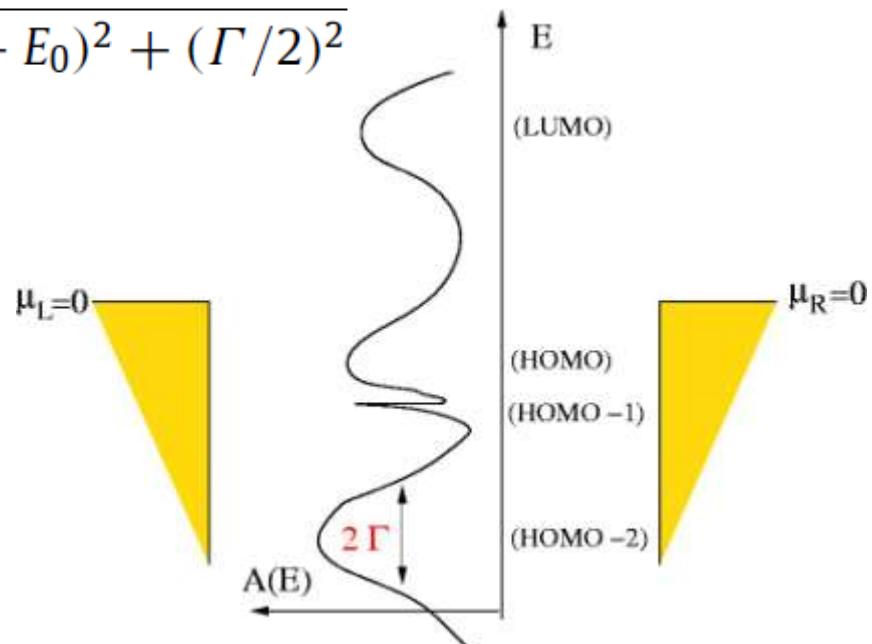
$$\Gamma = \Gamma_L + \Gamma_R$$

relate  $\Gamma$  to typical resilience time  $\tau$ :

Heisenberg       $\Delta E \Delta t > \hbar$

hence             $\Gamma = \hbar/\tau$

- **shift:** equil.  $\Leftrightarrow$  charge transfer  
typ. from electrode to molecule



# "good" contact

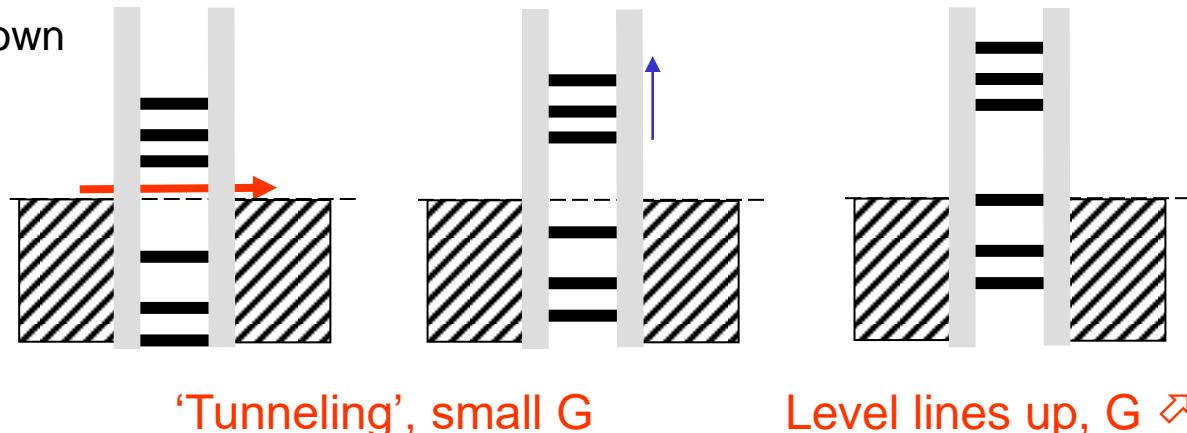
## current

- molecule seen as scatterer (Landauer)
  - ⇒ def. transmission function  $T(E)$   
molecular orbitals  $\Leftrightarrow$  peaks in  $T(E)$

$$I(E, V) = \frac{2e}{h} \int_{-\infty}^{\infty} \overline{T}(E, V) [f(E - \mu_2) - f(E - \mu_1)] dE$$

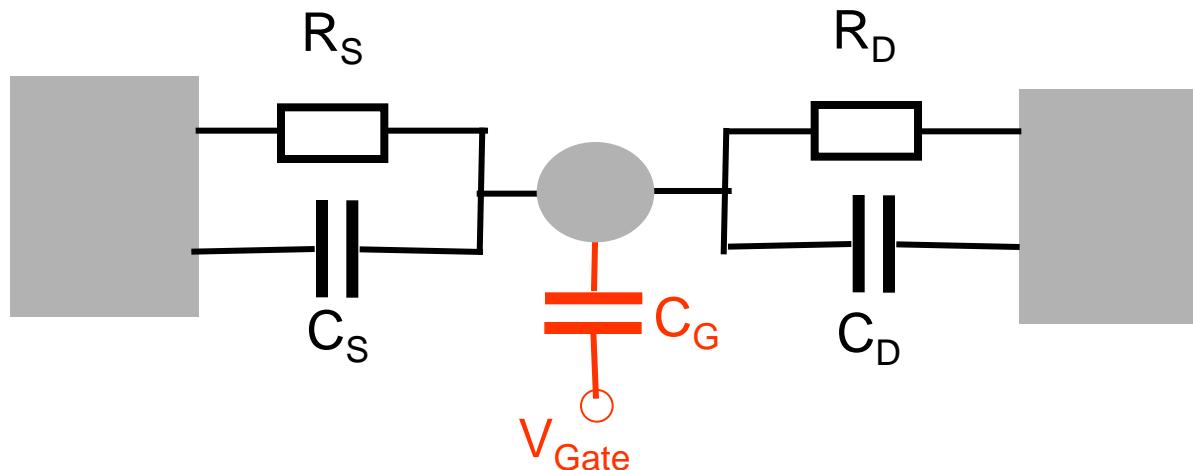
current ~ transmission probability x nb of states

- at low bias:  
 $E_F$  in HOMO-LUMO gap,  $I$  and  $G=U/I$  small
- gating: moving levels up/down



"bad" contact  $\Leftrightarrow$  capacitance

**Equivalent circuit, R large, C small**



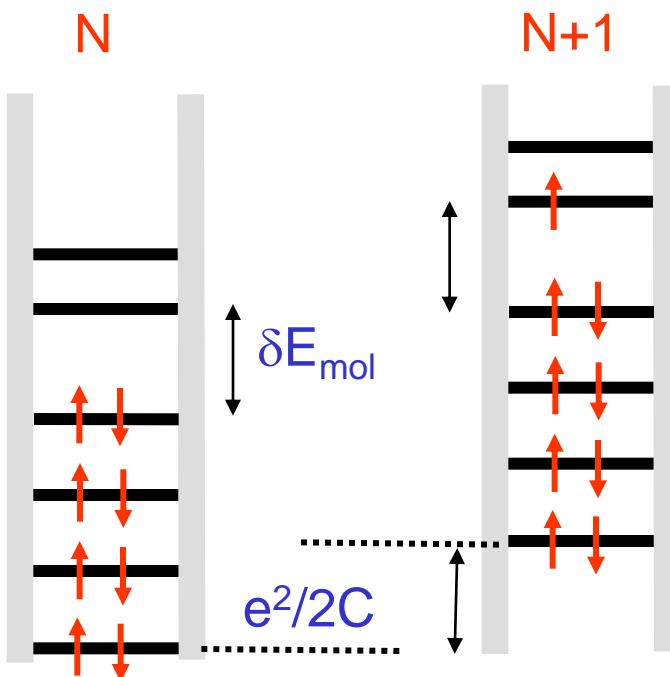
1. Residence time  $e^-$ :  $\Delta t = R_t C$
2. Charging energy  $e^-$ :  $E_C = e^2/2C$

# Coulomb Blockade

If

$$E_C = e^2/2C \gg k_B T$$

Then: Charging by one electron  
changes **all** energy levels!



Transport only if  
 $eV > \delta E_{\text{mol}} + e^2/2C$   
'Coulomb blockade'

# contacts

**too weak coupling:** like semiconductors qdots

boring for molecular electronics...

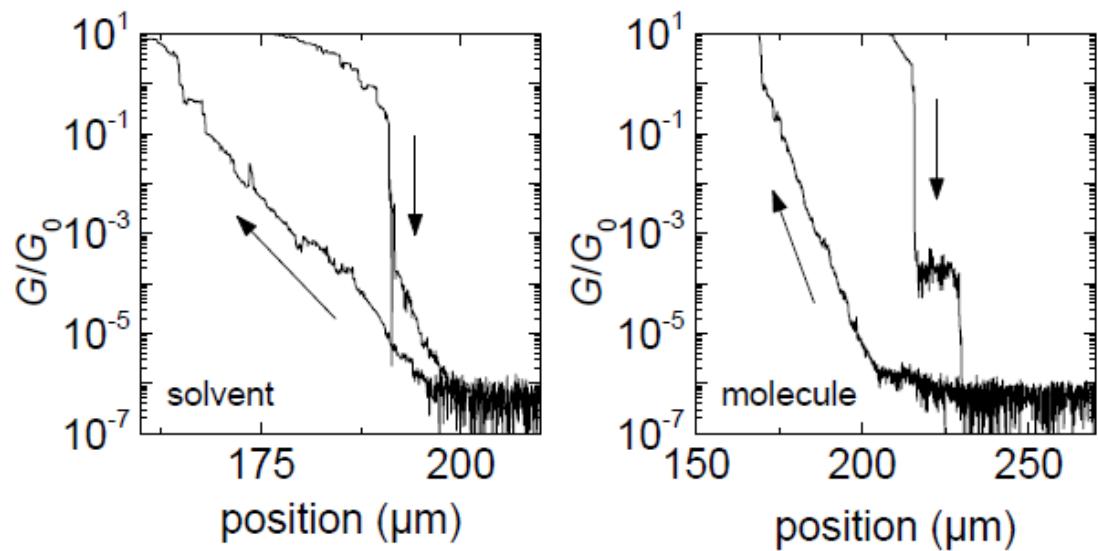
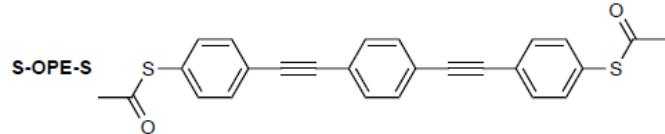
*rather work with a GaAs structure, more stable and reproducible*

**too strong coupling:** loose molecular signature... boring again

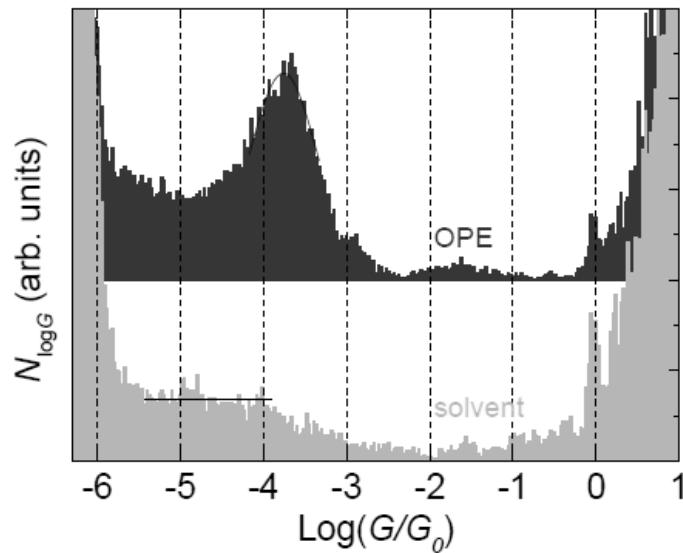
- ⇒ **control coupling to preserve integrity of molecular orbitals**  
in particular for **active** devices (otherwise, loss of functionality)

conjugated  
molecules

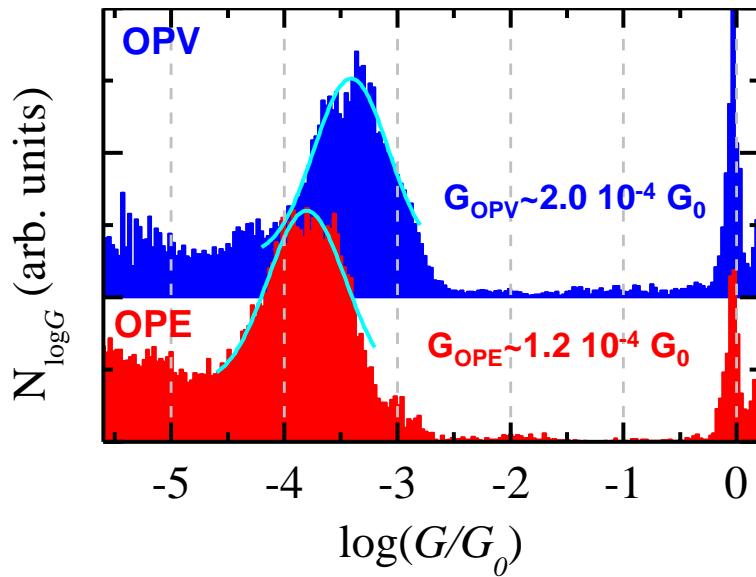
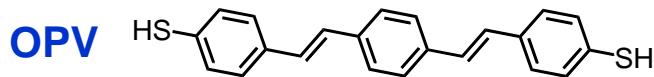
# molecular junction in a break junction



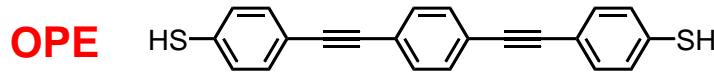
**statistical approach**



# conjugated systems



**simplified description**  
elastic, coherent tunneling,  
no  $e^-e^-$ , no  $e^-ph$



**NB: acetyl-protected molecule: deprotection necessary**

- experimental data       $G_{\text{OPV}} / G_{\text{OPE}} \sim 1.7$

- theory\*  $G_{\text{OPV}} / G_{\text{OPE}} \sim 2$

*NB:*

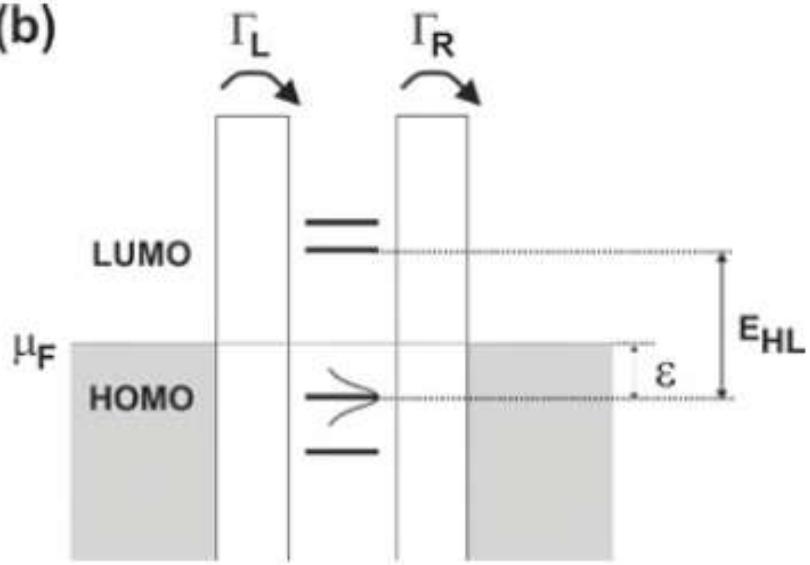
calc.

$$G_{OPV}/G_{OPE} \sim 2$$

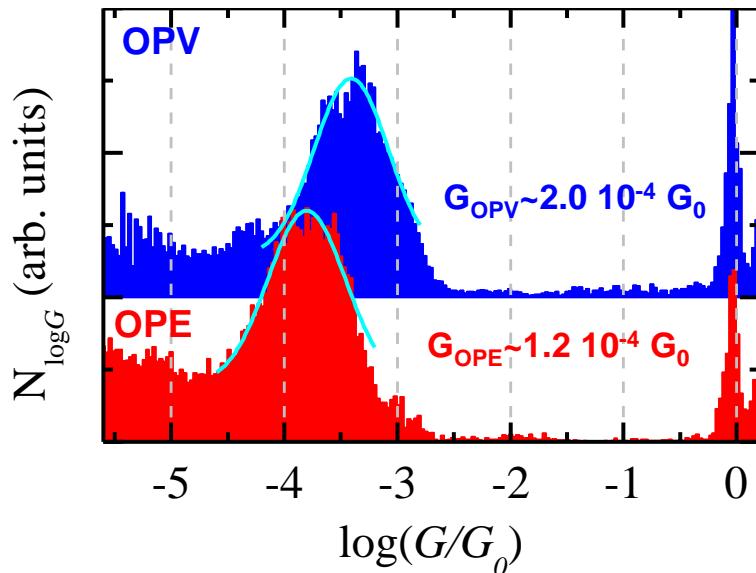
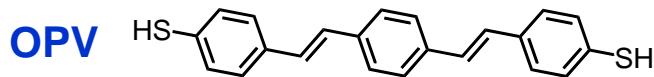
$$G_{OPE} \sim 10-200nS$$

*meas.*  $G_{OPE} \sim 10nS$

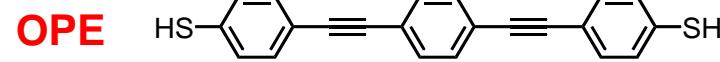
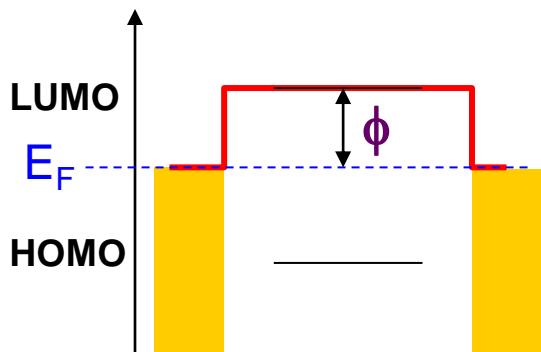
(b)



# conjugated systems



- single-step through-molecule tunneling



NB: acetyl-protected molecule: deprotection necessary

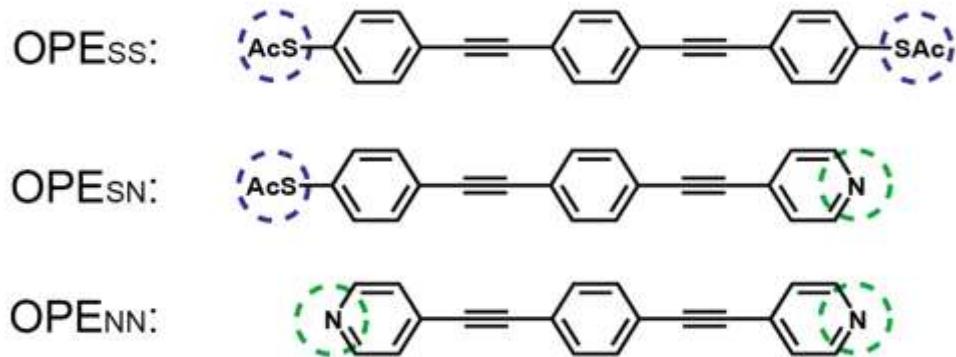
- experimental data  $G_{OPV} / G_{OPE} \sim 1.7$
- theory\*  $G_{OPV} / G_{OPE} \sim 2$   
NB:  
calc.  $G_{OPE} \sim 10\text{-}200\text{nS}$   
meas.  $G_{OPE} \sim 10\text{nS}$
- simple estimate  $G_{OPV} / G_{OPE} \sim 3.6$

$$G = Ae^{-\beta d}$$

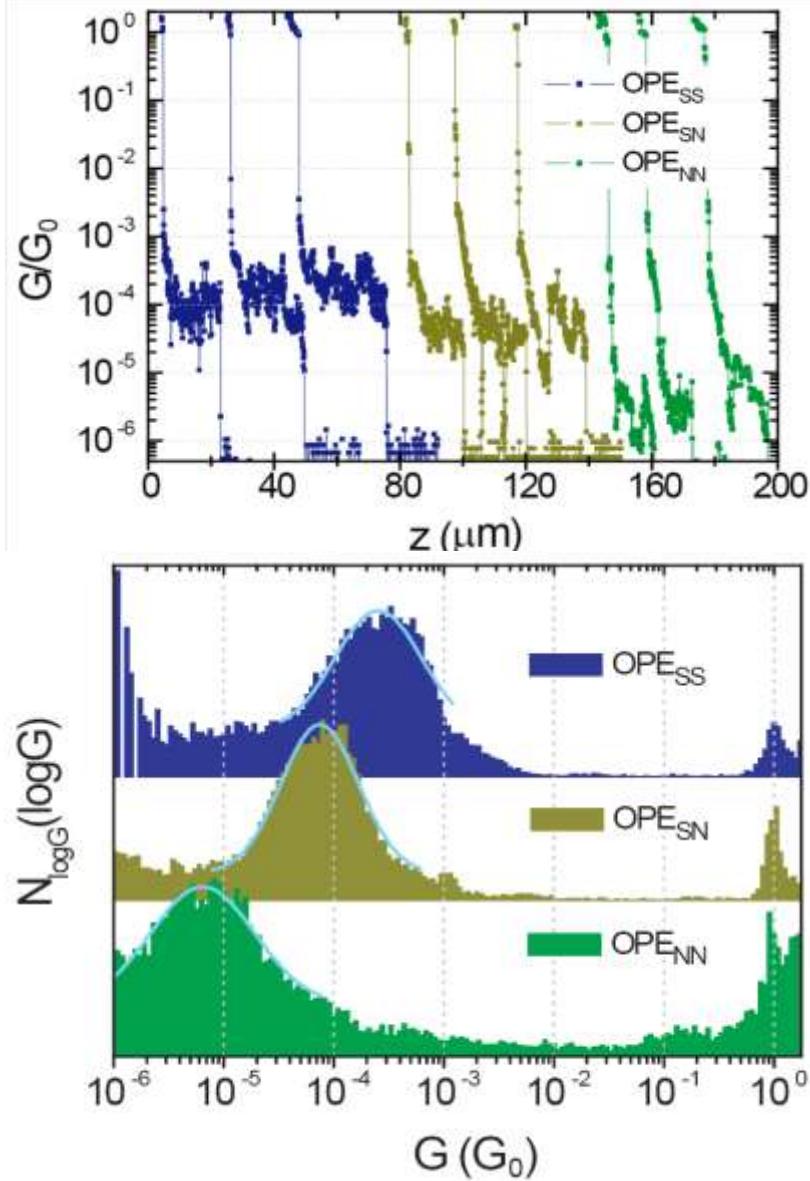
$$\beta \propto \sqrt{\phi} \propto \sqrt{\frac{|E_{LUMO} - E_{HOMO}|}{2}}$$

**d** molecule length  
**A**  $\sim G_0$  (1st approx.)  
*(A: linked to Au-S bond)*

# contacts: thiols and pyridines



Molecule	No. of samples	G ( $G_0$ )	Length (Å)
OPE <sub>SS</sub>	4	(1)	20.7 (S,S)
OPE <sub>SN</sub>	3	(1/2)	18.7 (S,N)
OPE <sub>NN</sub>	4	(1/35)	16.6 (N,N)



# contacts: thiols and pyridines

simple tunneling model:

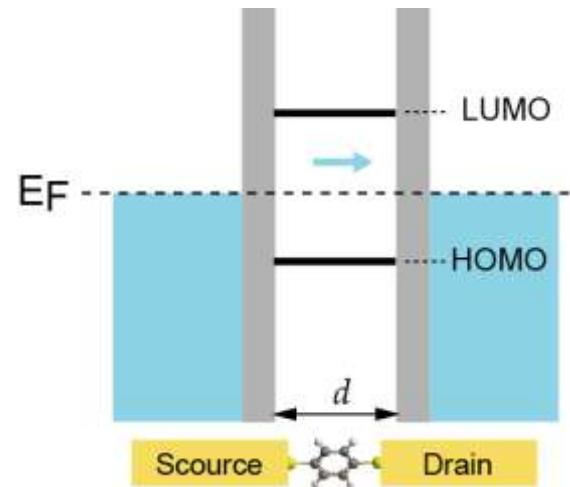
$$G = A_{left} \cdot A_{right} \cdot e^{-\beta d}$$

$\beta$ : decay constant ( $\beta_{OPE} = 0.3 \text{ \AA}^{-1}$ )

$d$ : length of molecule

$A$ : contact conductance

Frisbie et al., JACS (2002), Tao et al., JACS (2006)



## ***symmetric***

$$\text{OPE-SS: } G_{ss} = A_s^2 \cdot e^{-\beta d_{ss}}$$

contact  $\sim 54 \text{ k}\Omega^1$

$$\text{OPE-NN: } G_{nn} = A_n^2 \cdot e^{-\beta d_{nn}}$$

contact  $\sim 460 \text{ k}\Omega^1$

## ***asymmetric***

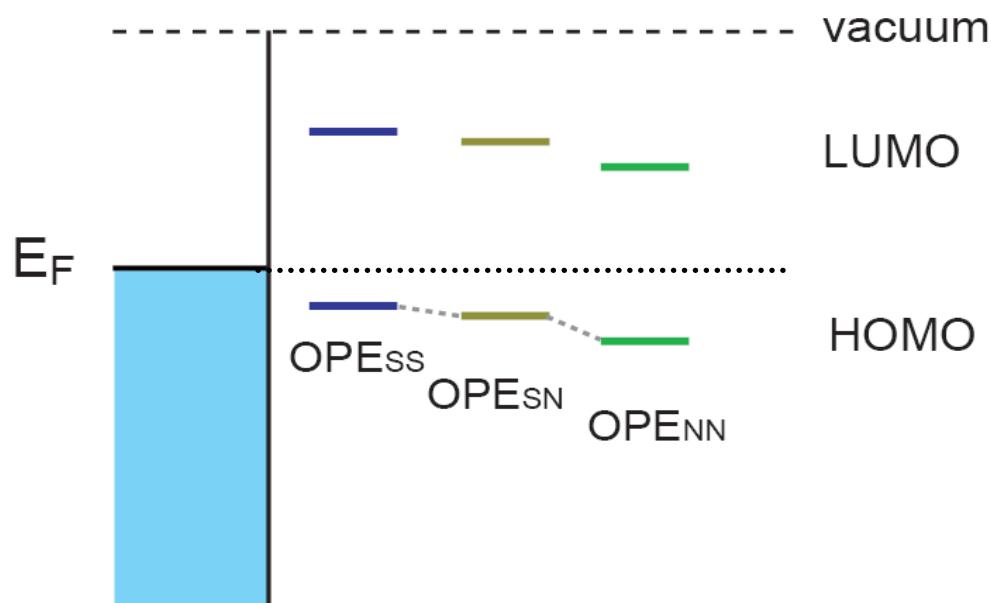
$$\text{OPE-SN: } G_{sn} = A_s \cdot A_n \cdot e^{-\beta d_{sn}}$$

discrepancy ( $\sim x3$ ) between measured and value anticipated from meas. above

⇒ simple tunneling model does not hold

⇒ for asymmetric OPE-SN, thiol anchors dominate

# contacts: level alignment



## calculations

(alkanedithiols, alkanediamines)

dominant orbital: HOMO

dithiol  $E_H - E_F \sim 2\text{eV}$

diamine  $E_H - E_F \sim 3\text{eV}$

( $E_{HL} \sim 8\text{eV}$ )

McDermott et al., J. Phys. Chem. C (2009)

⇒ spectroscopic measurement ?

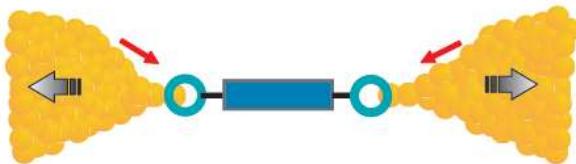
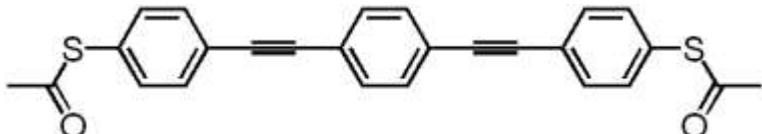
**upon binding** charge transfer, level alignment

S-Au strong covalent bonding (-δ on S) ⇒  $|E_F - E_H| \searrow, G \nearrow$

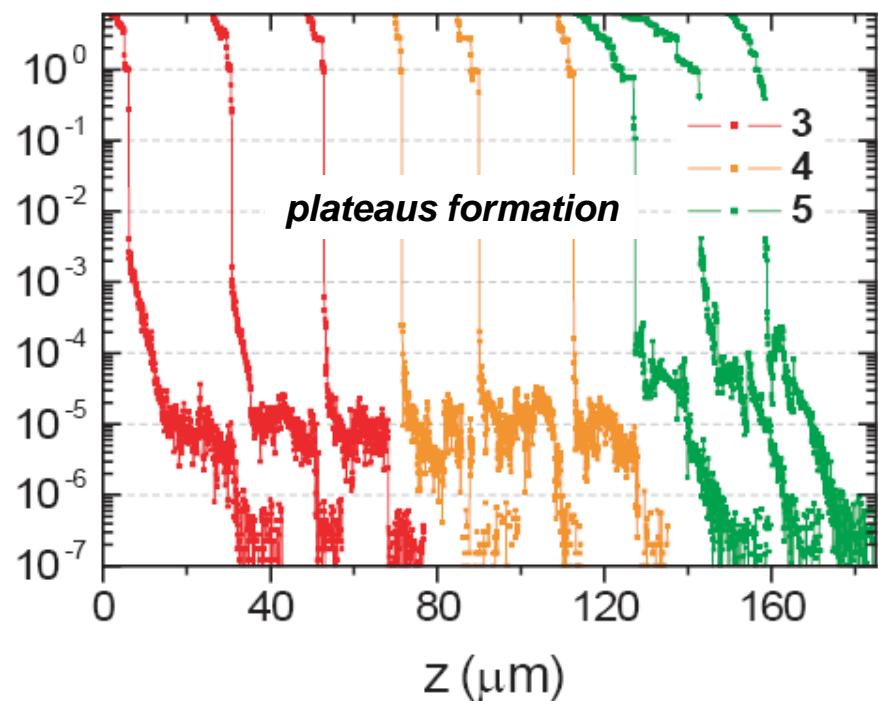
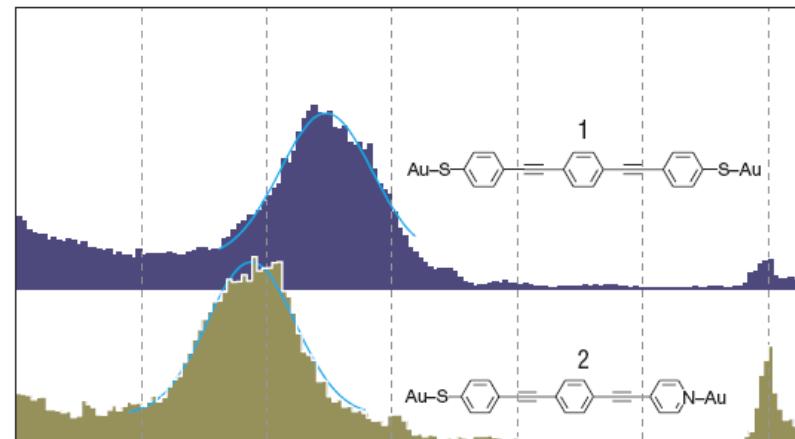
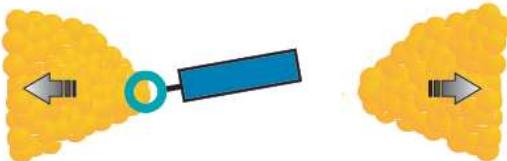
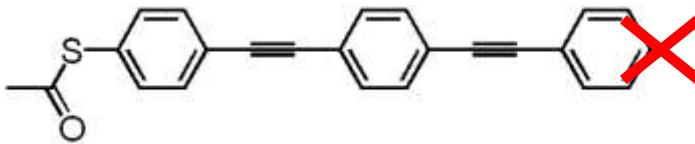
Pyridine N-Au weak donor-acceptor bonding (+δ on N) ⇒  $|E_F - E_H| \nearrow, G \searrow$

# importance of intermolecular interactions

OPE: oligo (phenylene ethynilene)

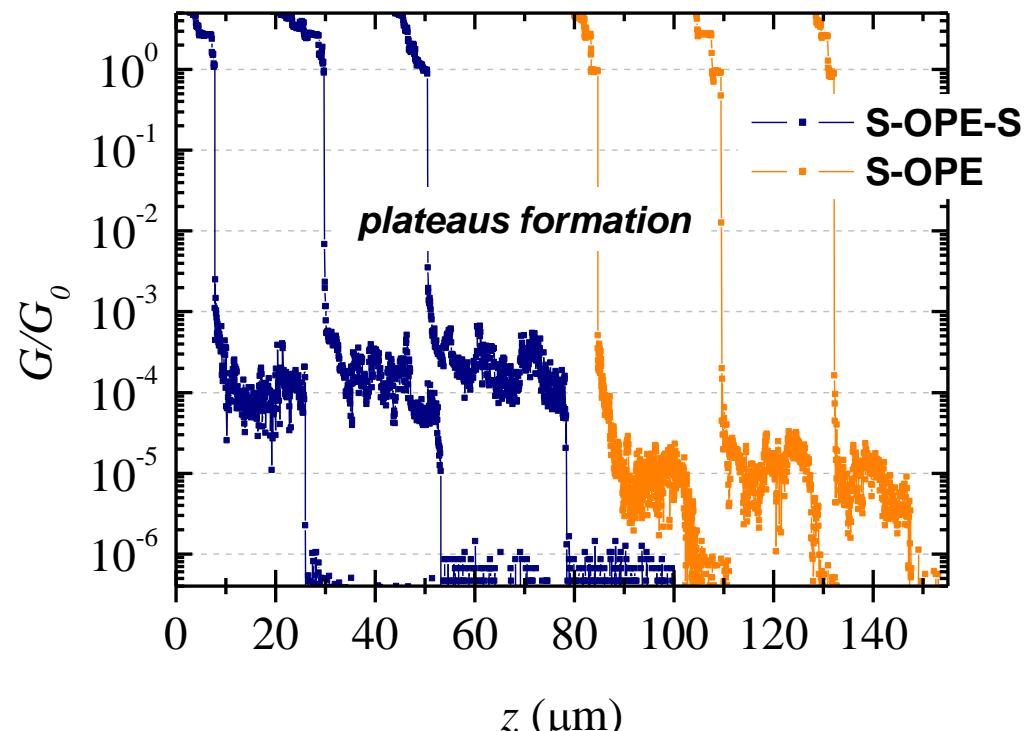
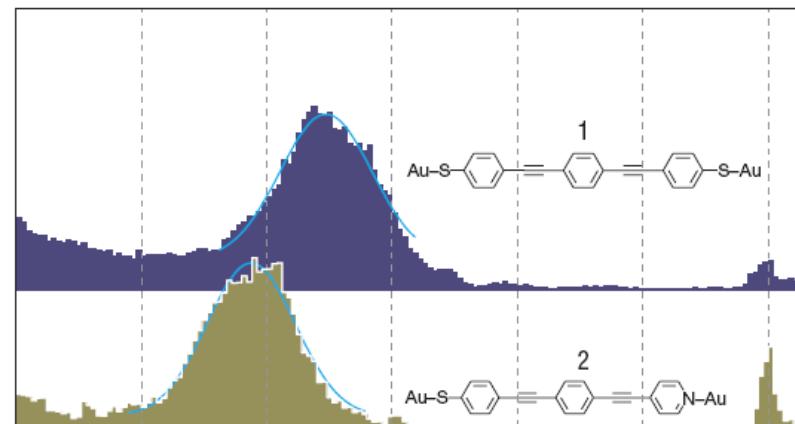
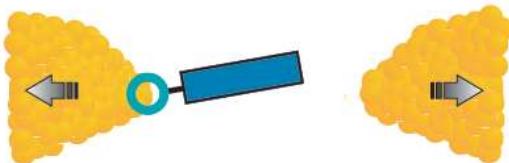
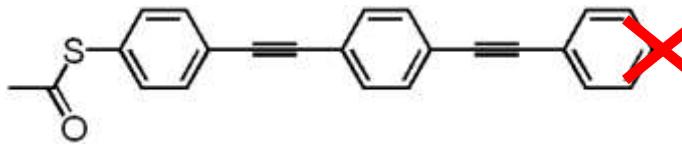
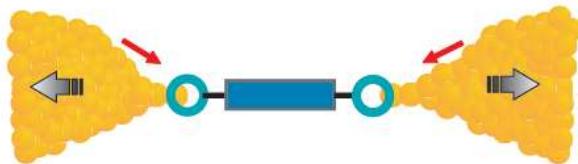
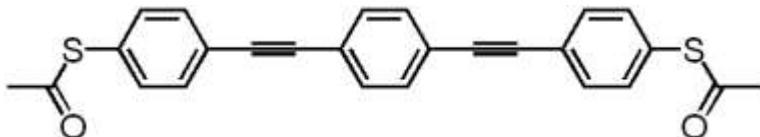


*what happens with a single anchor group ?*



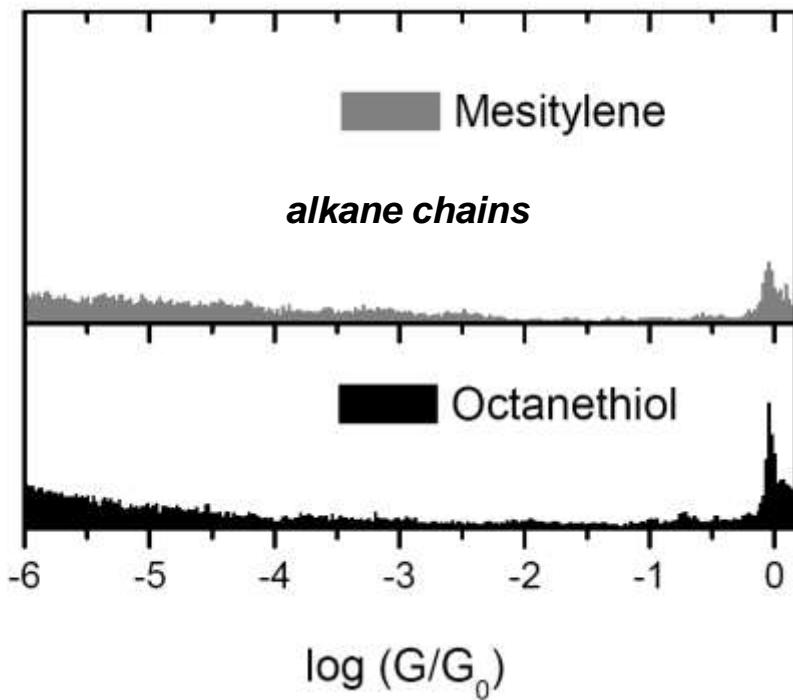
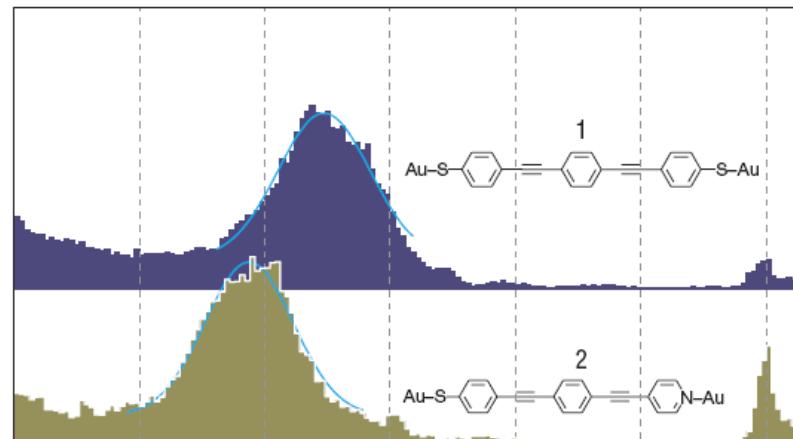
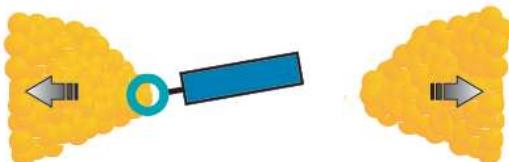
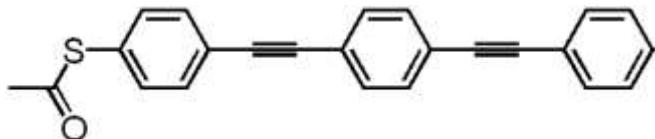
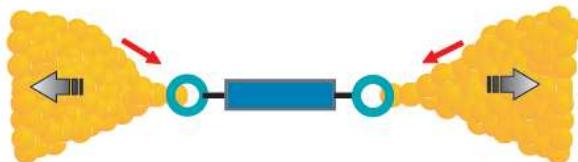
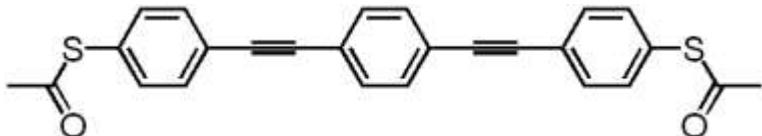
# importance of intermolecular interactions

OPE: oligo (phenylene ethynylene)



# importance of intermolecular interactions

**OPE:** oligo (phenylene ethynilene)



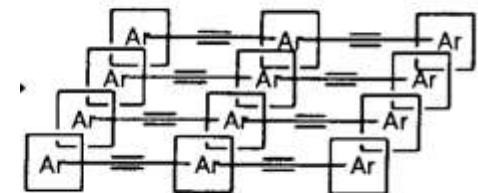
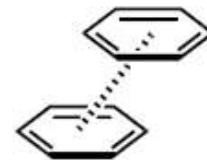
**molecules:** M. Mayor, Basel

# importance of intermolecular interactions

## ↗ $\pi$ -stacking

aggregation of conjugated compounds

Burley et al., Science (1985); Hunter et al., JACS (1990), M. Levitus et al. JACS (2001)



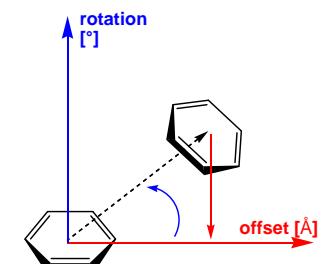
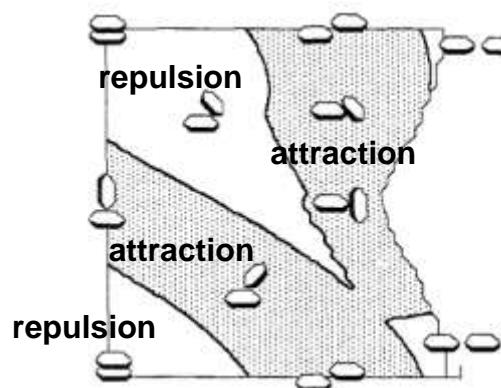
benzene-benzene interaction

E ~ 70meV to 100meV

~  $2.7 k_B T$  to  $4 k_B T$

~ 1.6 to 2.4 kcal/mol

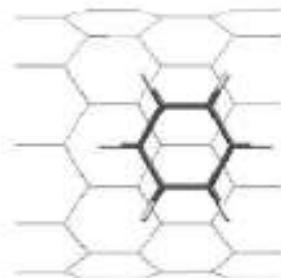
Jorgensen et al., JACS, 1990



benzene-CNT interaction

E ~ 0.1 – 0.2 eV

Tournus et al., PRB 2005; Zhao et al., APL 2003

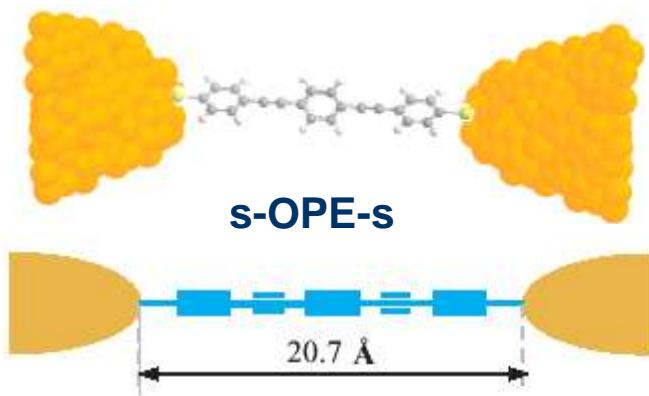
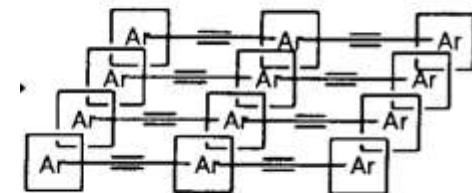
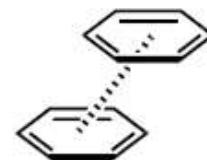


# importance of intermolecular interactions

## ↗ $\pi$ -stacking

aggregation of conjugated compounds

Burley et al., Science (1985); Hunter et al., JACS (1990), M. Levitus et al. JACS (2001)



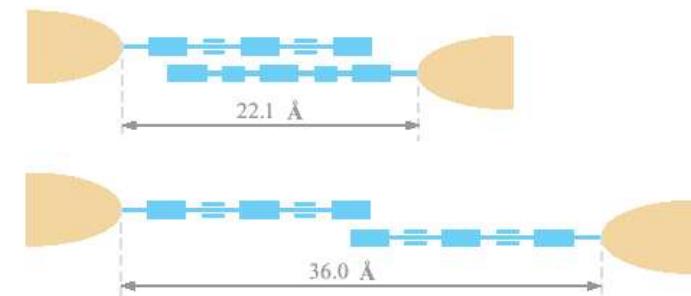
- experimental data  $G_{\text{sOPE}} / G_{\text{sOPEs}} = 20$

- $G = Ae^{-\beta d}$   $G_{\text{sOPEs}}/G_{\text{sOPE}} = 12$

$d$  = molecule length

$A$  = contact conductance

$\beta$  = decay constant, for OPE:  $\beta_{\text{OPE}} = 0.3 \text{ \AA}^{-1}$

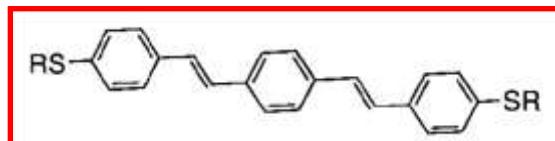
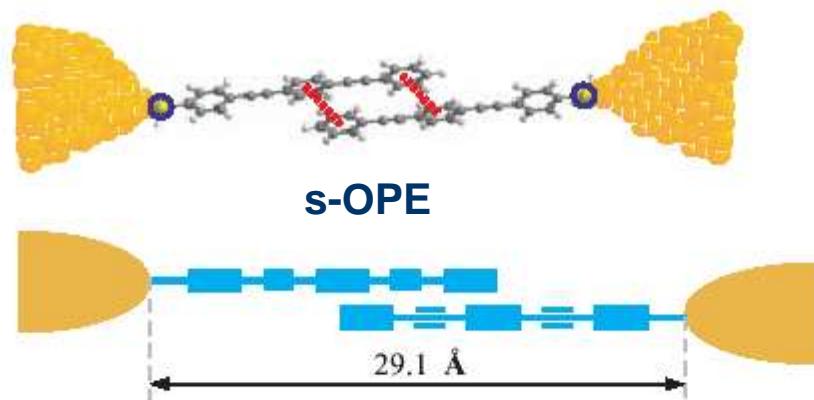
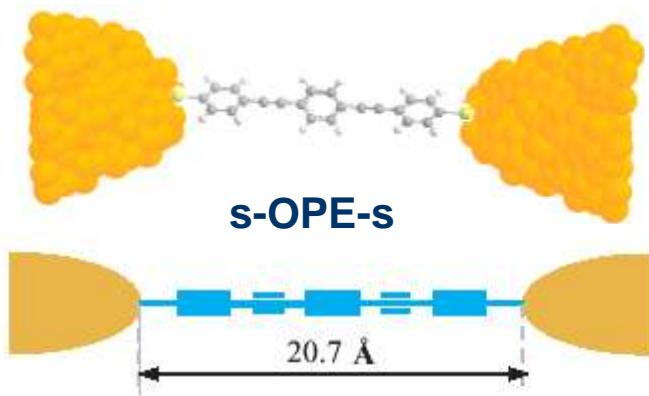
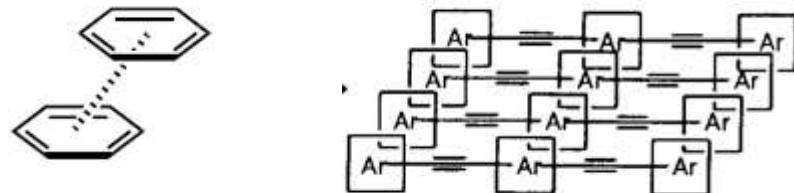


# importance of intermolecular interactions

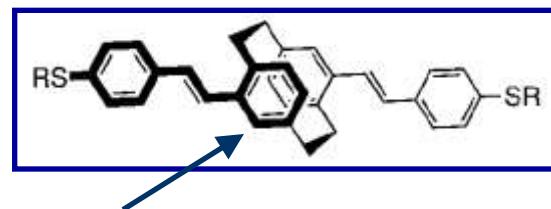
## ↗ $\pi$ -stacking

aggregation of conjugated compounds

Burley et al., Science (1985); Hunter et al., JACS (1990), M. Levitus et al. JACS (2001)



≈ equivalent to

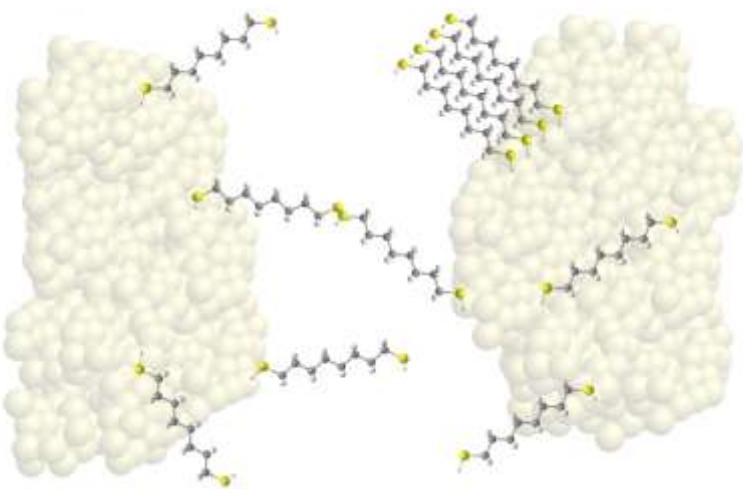


strong through-space  $\pi$ -conjugation

D. S. Seferos, J. G. Kushmerick et al. PNAS (2005)

# spectroscopy

# molecular junction formation

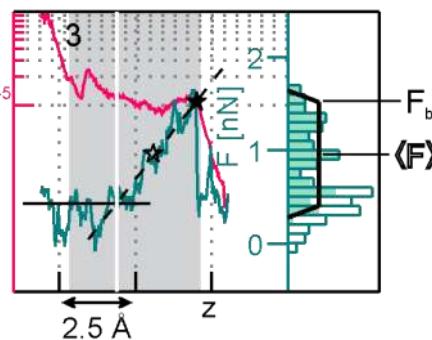
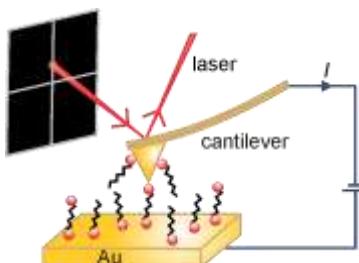


*drifting molecules,  
stochastic anchoring,  
random clustering*  $\Rightarrow$  *undefined junction  
geometry &  
conductance*

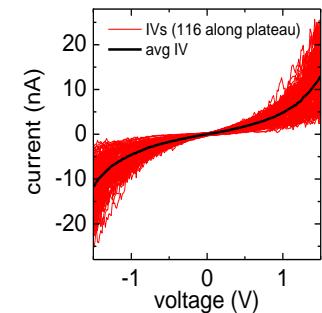
*drifting surface  
atoms, metal  
protrusions*  $\Rightarrow$  *undefined  
electrostatic  
landscape*

$\Rightarrow$  **variability, low-yield and lack of control in key electrical parameters**

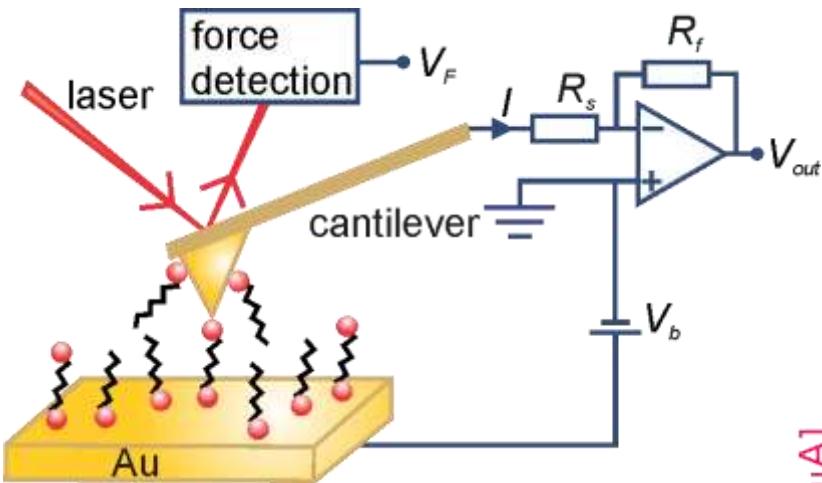
## force spectroscopy force-conductance correlation



## current-voltage spectroscopy fast IV characteristics in the non-linear regime



# octanedithiol junctions investigated by C-AFM



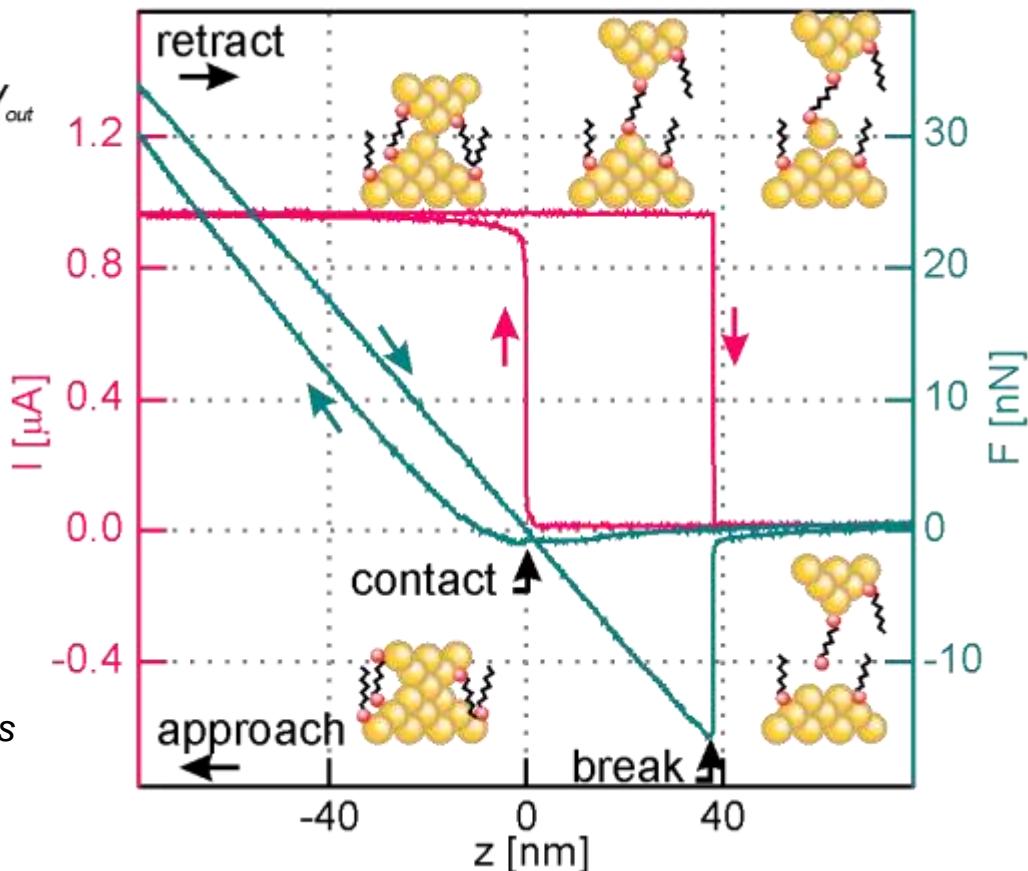
**substrate:** Au on SiO<sub>2</sub>/Si  
**cantilever:** Si, Au-coated  
typ. 4 N/m

*NB: both surfaces coated with alkanes monothiols*

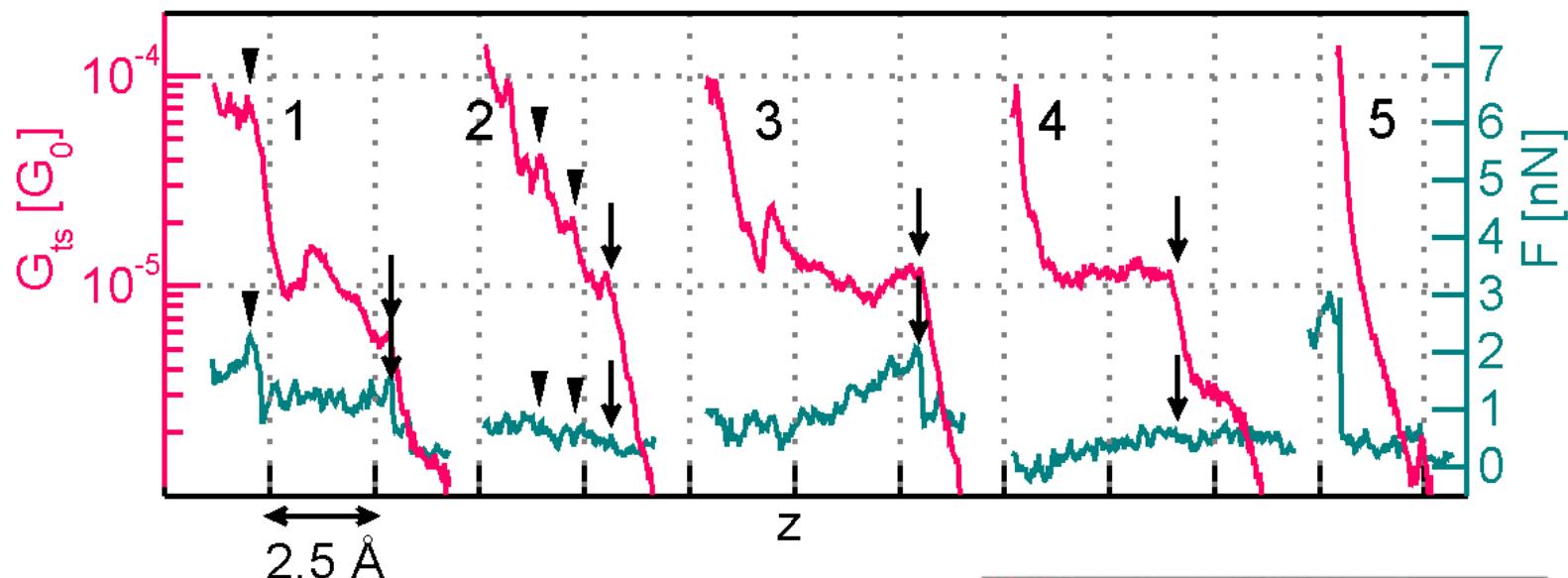
**approach:** ~ 200nm/s, Fmax: 15nN for  
Au-molecule-Au junctions

**retraction:** ~15nm/s

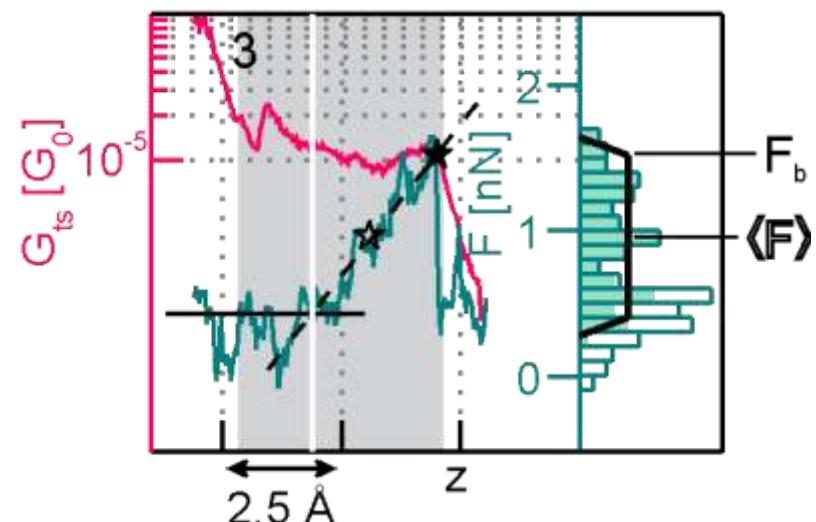
**environment:** mesitylene



# retraction curves: octanedithiols junctions



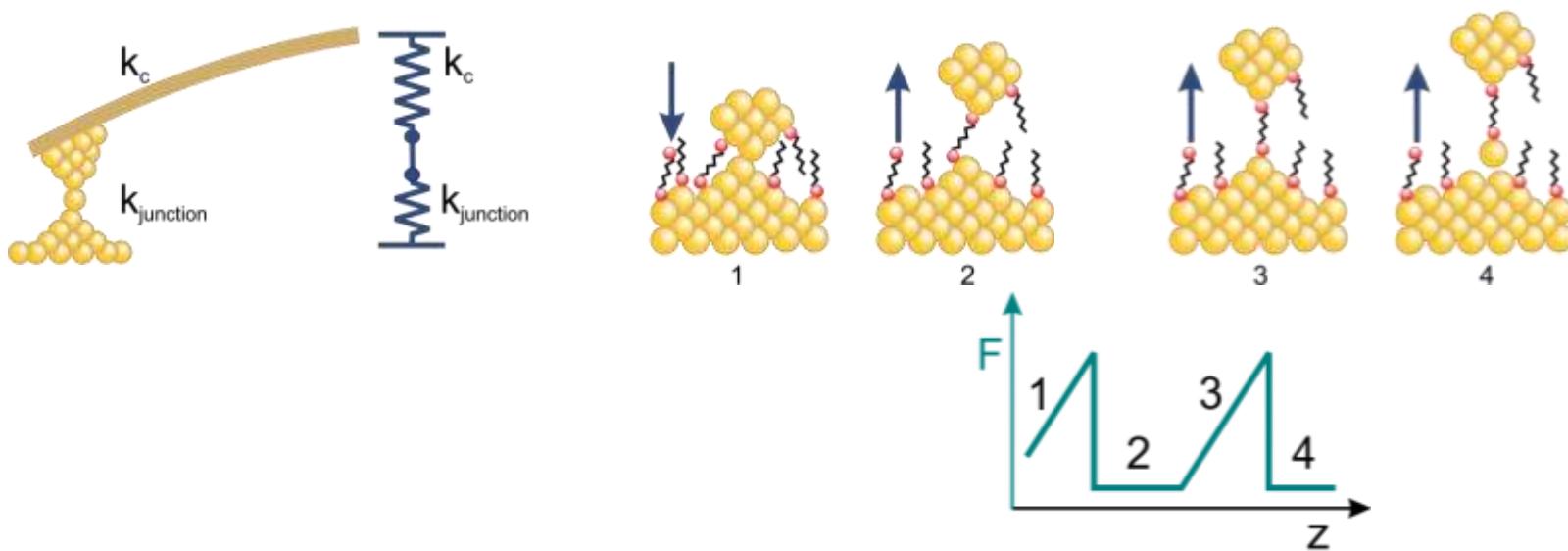
- **last  $G$  plateau close to  $10^{-5} G_0$**
- **curve 3 (20%):** dashed line:  $4.1 \text{ N/m}$   
( $k_c$  of cantilever:  $4.2 \text{ N/m}$ )
- **force histogram**
  - ★: breaking force  $F_b$   
( $1.5 nN$  here)
  - ☆: mean force  $\langle F \rangle$



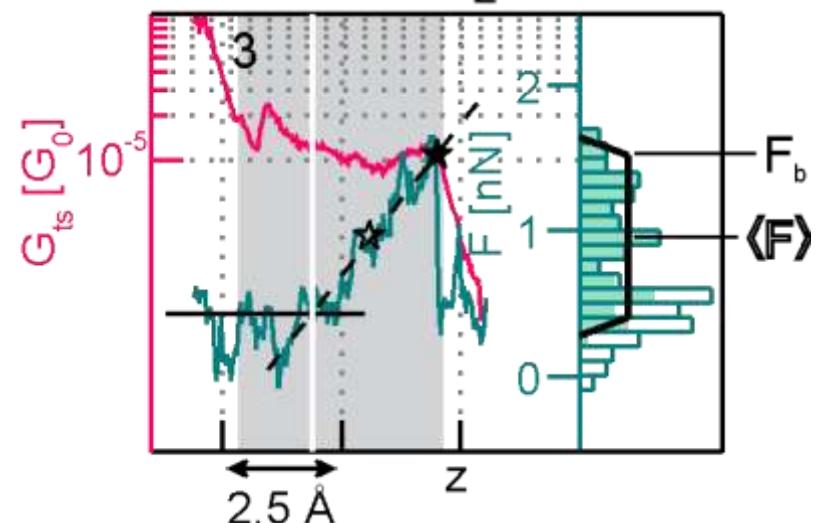
**NB:** noiseless  $F$  curve  $\Leftrightarrow$  rectangular force histo

C. Nef et al.

# retraction curves: octanedithiols junctions



- last G plateau close to  $10^{-5} G_0$
- curve 3 (20%): dashed line:  $4.1 \text{ N/m}$   
( $k_c$  of cantilever:  $4.2 \text{ N/m}$ )
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★: breaking force  $F_b$   
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- mean force  $\langle F \rangle$



**NB:** noiseless F curve  $\Leftrightarrow$  rectangular force histo

C. Nef et al.

# octanedithiols junctions: scatter plot (2D histo)

## 2D histogram for 1 pair of (G,F) curves

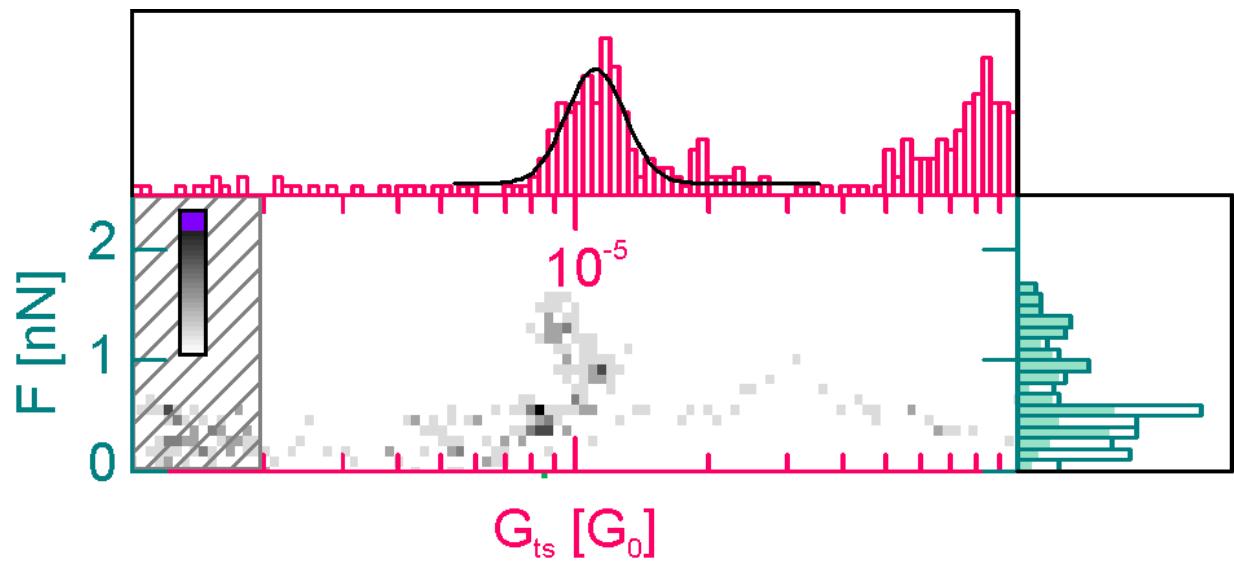
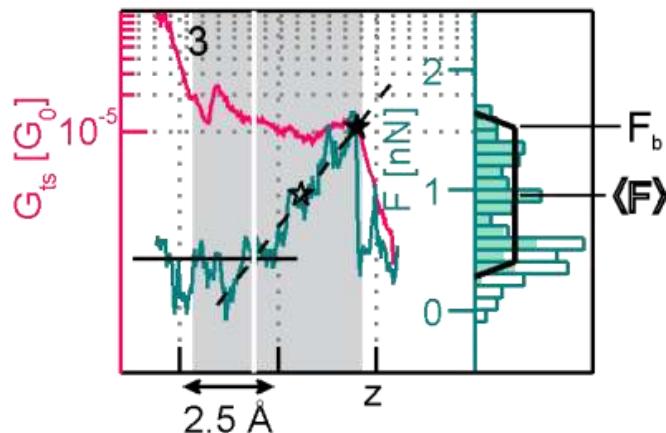
- data from pulling ( $F > 0$ )
- binning of G and F

$$\Delta \log(G_{ts}/G_0) = 0.02$$

$$\Delta F = 100 \text{ pN}$$

- building the 2D histo:

*(1 point in G curve and its corresponding point in F curve contribute 1 count in the 2D histo at the correponding bin)*



# octanedithiols junctions: scatter plot (2D histo)

**G histo: peak**

$$G_{\text{mol}} \approx 1.1 \cdot 10^{-5} G_0$$

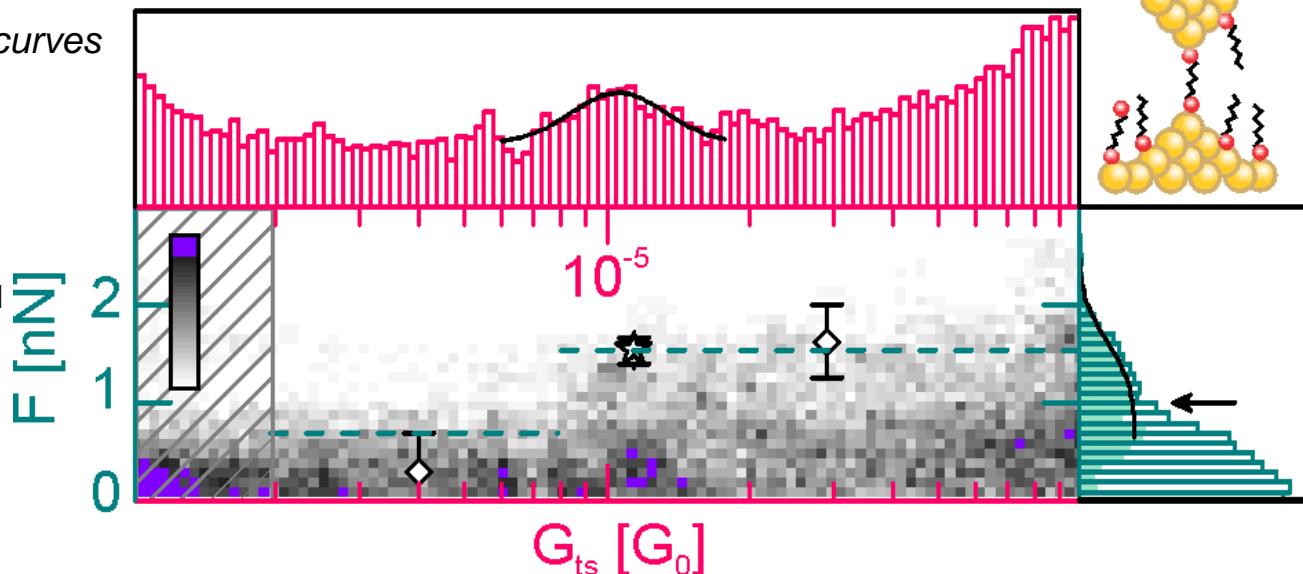
**F range: jump at  $0.8 G_{\text{mol}}$**

dashed lines: 0.7 nN & 1.6 nN

$\diamond: \langle F \rangle \sim 0.3 \text{nN}$

for  $G < 8 \cdot 10^{-6} G_0$

115 ( $G, F$ ) curves



# octanedithiols junctions: scatter plot (2D histo)

**G histo: peak**

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$\diamond$ :  $\langle F \rangle \sim 0.3 \text{nN}$

for  $G < 8 \cdot 10^{-6} G_0$

$\diamond$ :  $\langle F_b \rangle \sim 1.6 \text{nN}$

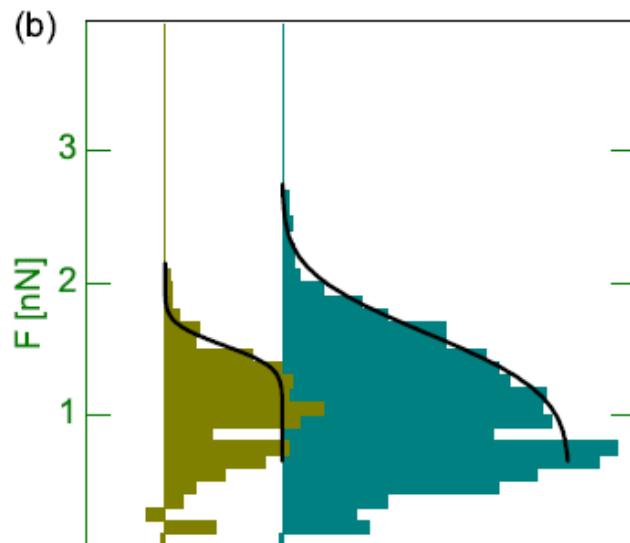
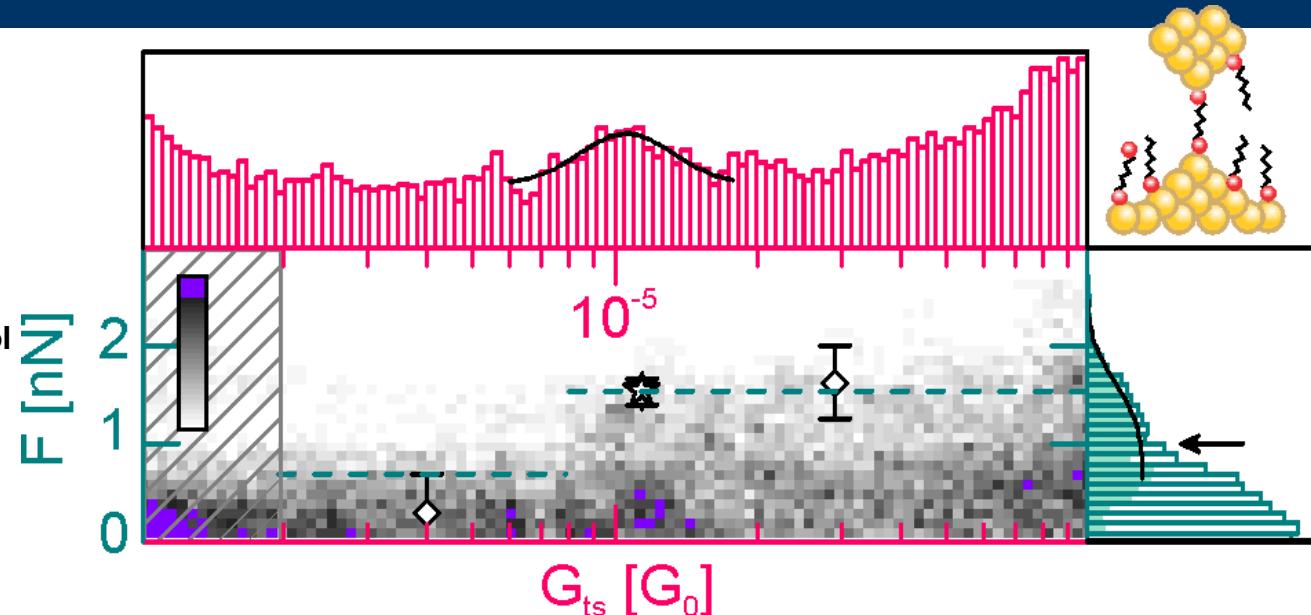
for  $G > 8 \cdot 10^{-6} G_0$

$\star$ :  $\langle F_b \rangle \approx 1.5 \pm 0.1 \text{nN}$

mean breaking force

**around  $G_{\text{mol}}$**

( $0.8 - 1.6 \cdot 10^{-5} G_0$ )



$F_b$  normally distributed  $\Rightarrow$

$$F(x) = \frac{A}{\sqrt{2\pi}\sigma} \int_{-\infty}^x e^{-1/2(\frac{t-\mu}{\sigma})^2} dt$$

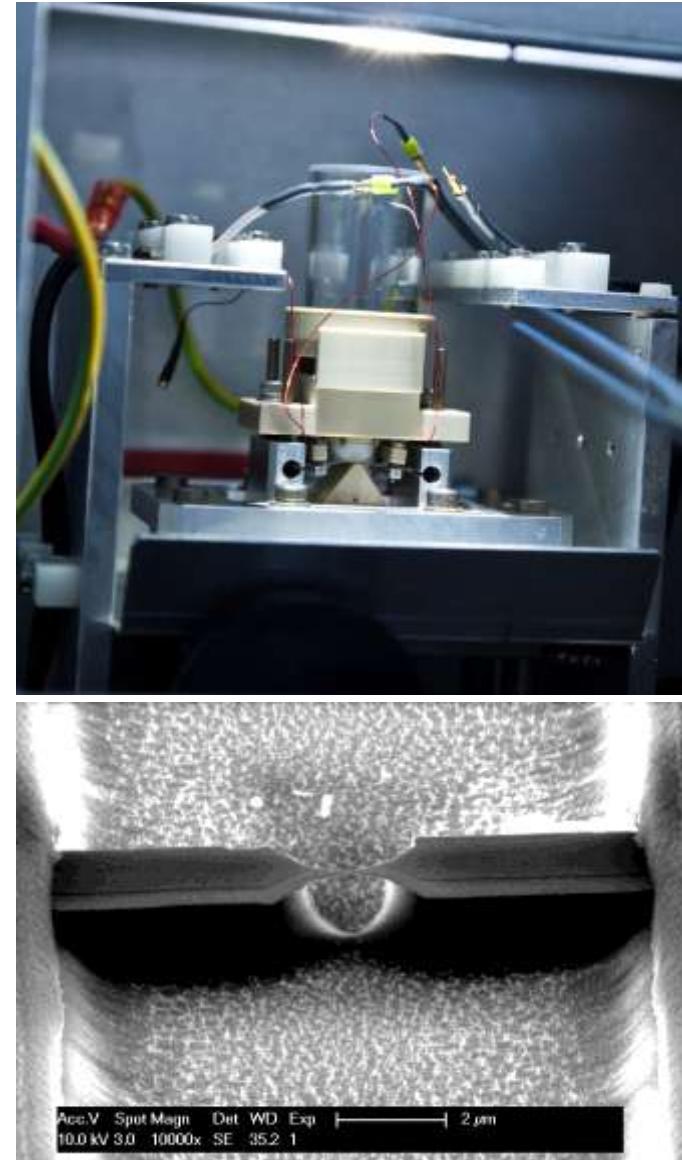
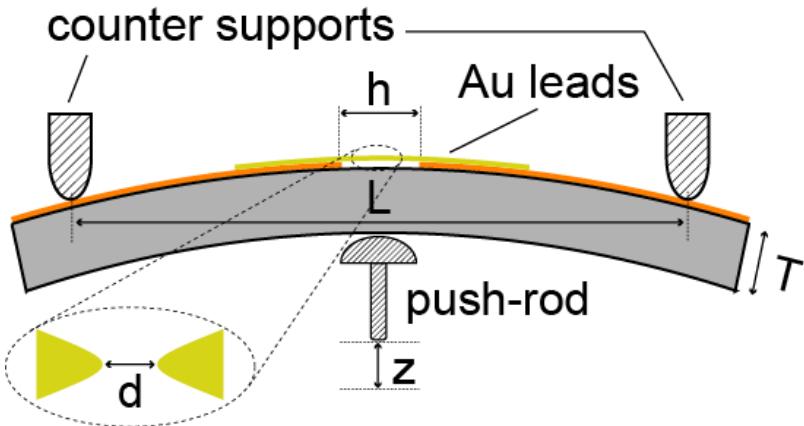
$$F(x) = \frac{A}{2} \left[ 1 + \operatorname{erf} \left( \frac{x-\mu}{\sqrt{2}\sigma} \right) \right]$$

$$\mu \Leftrightarrow \langle F_b \rangle$$

current-voltage  
spectroscopy

# current-voltage spectroscopy

## Mechanically controllable break junctions

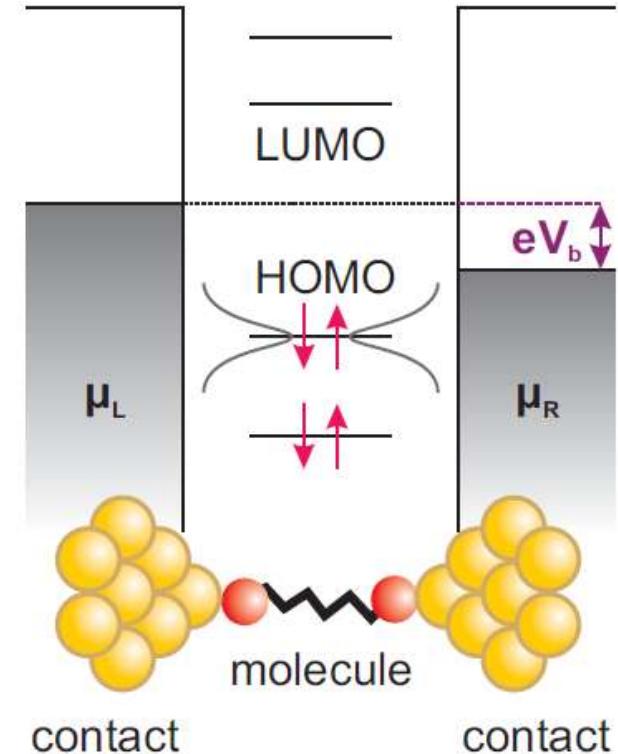
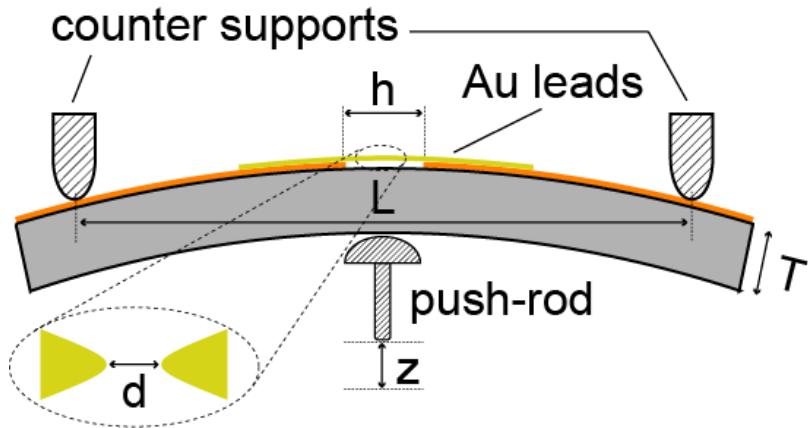


**Measurements** ramp V during opening cycles  
while recording I  
**1 IV in 10ms** (200pnts per IV)

**rate of opening** typ.  $1\text{ \AA/s}$   
*i.e.  $\sim 0.01\text{ \AA}$  motion during 1 IV*

# current-voltage spectroscopy

## Mechanically controllable break junctions

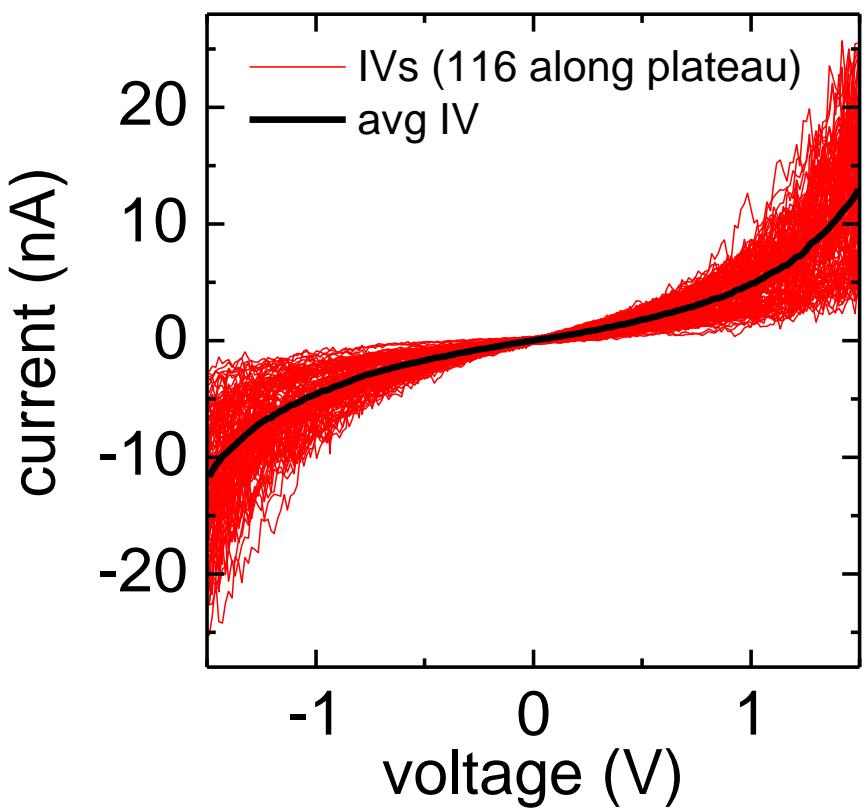


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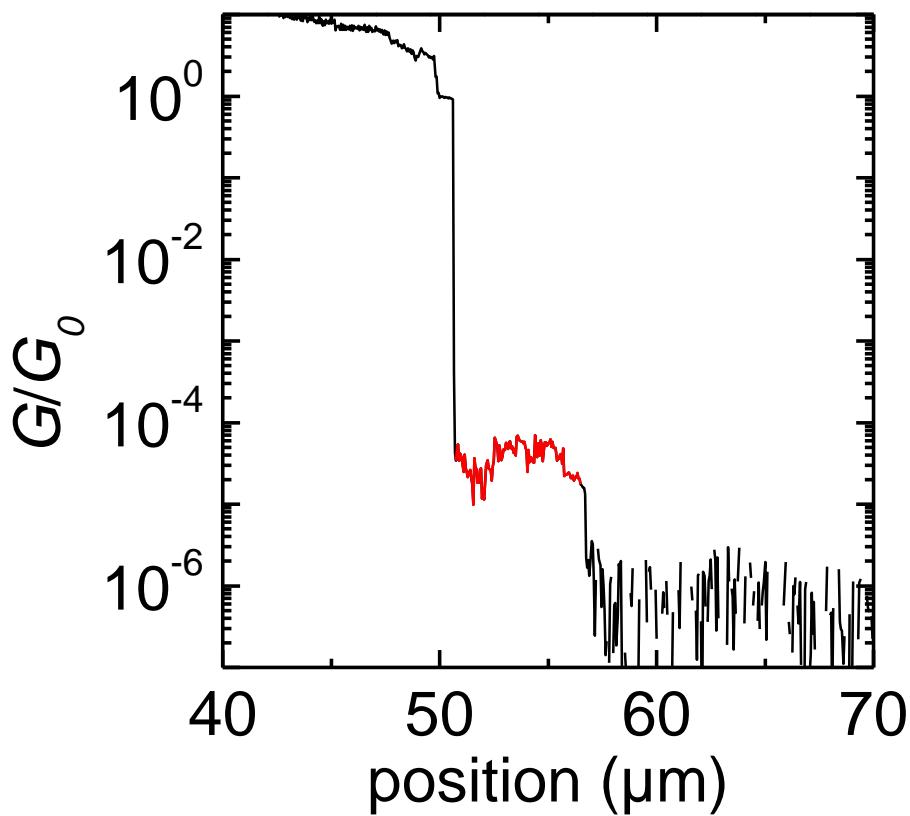
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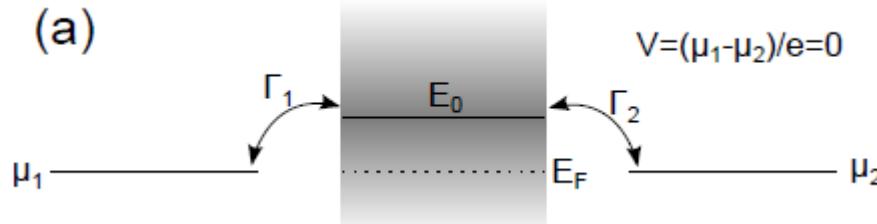
# IV characteristics in MCBJ



**G trace built from IV curves**  
*linear fit of IV curves in low-bias regime  
( $\pm 0.1$  V)*



# simple one-level model



$$I(E, V) = \frac{2e}{h} \int_{-\infty}^{\infty} T(E, V) [f(E - \mu_2) - f(E - \mu_1)] dE$$

**molecular level broadening: Lorentzian (Breit-Wigner)**

$$D_e(E) = \frac{(\Gamma_1 + \Gamma_2)/\pi}{(E - E_0(V))^2 + (\Gamma_1 + \Gamma_2)^2}$$

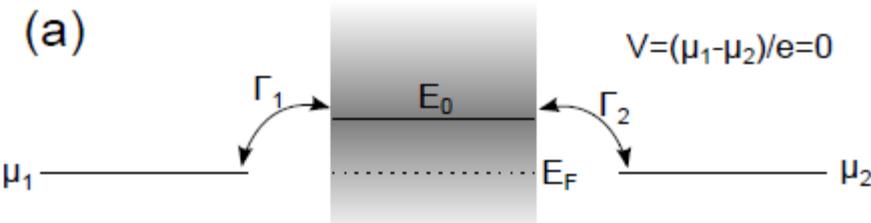
**transmission function from DOS and coupling constants**

$$T(E, V) = 4\pi D_e(E) \frac{\Gamma_1 \Gamma_2}{\Gamma_1 + \Gamma_2}$$

**and**       $T(E, V) = \frac{4\Gamma_1 \Gamma_2}{(E - E_0(V))^2 + (\Gamma_1 + \Gamma_2)^2}$

# simple one-level model

**voltage drop at contacts (asymmetric coupling):**  
forced to be  $\propto 1/\Gamma$



$$\frac{\frac{eV}{2} - E_F(V)}{\frac{eV}{2} + E_F(V)} \stackrel{!}{=} \frac{\Gamma_1^{-1}}{\Gamma_2^{-1}}$$

thus  $E_F(V) = \frac{eV}{2} \cdot \frac{\Gamma_1 - \Gamma_2}{\Gamma_1 + \Gamma_2}$

and we have, for the voltage-dependent molecular level position

$$E_0(V) = E_0 + E_F(V) = E_0 + \frac{eV}{2} \cdot \frac{\Gamma_1 - \Gamma_2}{\Gamma_1 + \Gamma_2}$$

The amount of shift for  $E_F$  is weighted by the coupling constants: the level shifts towards the better coupled electrode.

Boundary conditions

$$E_F = 0 \text{ for } \Gamma_1 = \Gamma_2$$

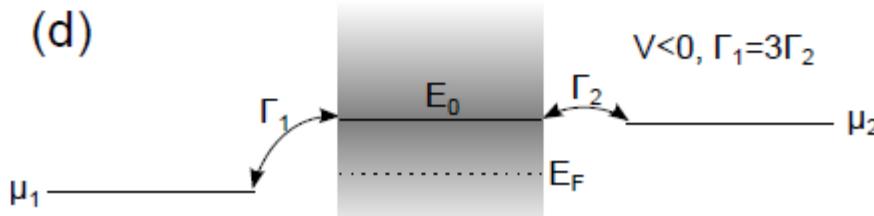
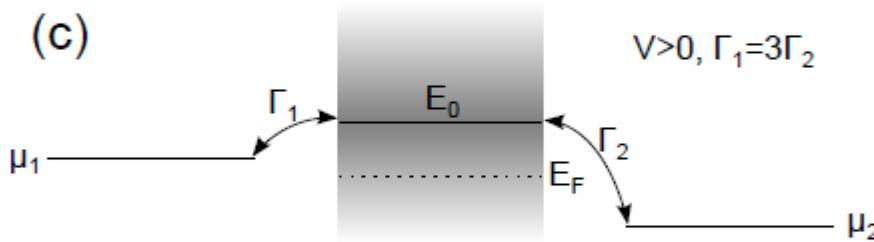
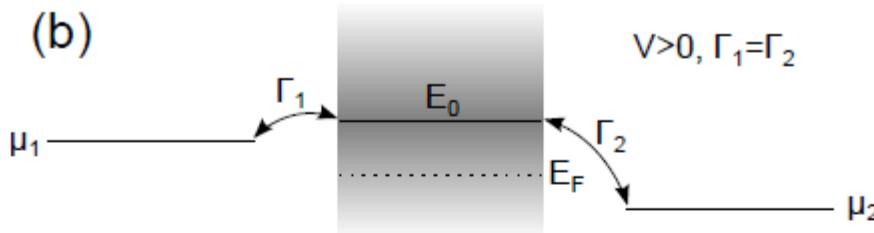
$$E_F = eV/2 = \mu_1 \text{ for } \Gamma_1 \gg \Gamma_2$$

$$E_F = \mu_2 \text{ for } \Gamma_2 \gg \Gamma_1$$

# simple one-level model

$$E_0(V) = E_0 + E_F(V) = E_0 + \frac{eV}{2} \cdot \frac{\Gamma_1 - \Gamma_2}{\Gamma_1 + \Gamma_2}$$

examples of  $E_F$  shift



# simple one-level model

**Analytical expression for the current**  $I(E, V) = \frac{2e}{h} \int_{-\infty}^{\infty} T(E, V)[f(E - \mu_2) - f(E - \mu_1)]dE$

**At low  $T$ , Fermi functions  $\approx$  Heaviside step functions, and**  $I(V) = \frac{2e}{h} \int_{\frac{-eV}{2}}^{\frac{eV}{2}} T(E, V)dE$

**Using the expressions**

$$T(E, V) = \frac{4\Gamma_1\Gamma_2}{(E - E_0(V))^2 + (\Gamma_1 + \Gamma_2)^2}$$

$$E_F(V) = \frac{eV}{2} \cdot \frac{\Gamma_1 - \Gamma_2}{\Gamma_1 + \Gamma_2}$$

**we can write**

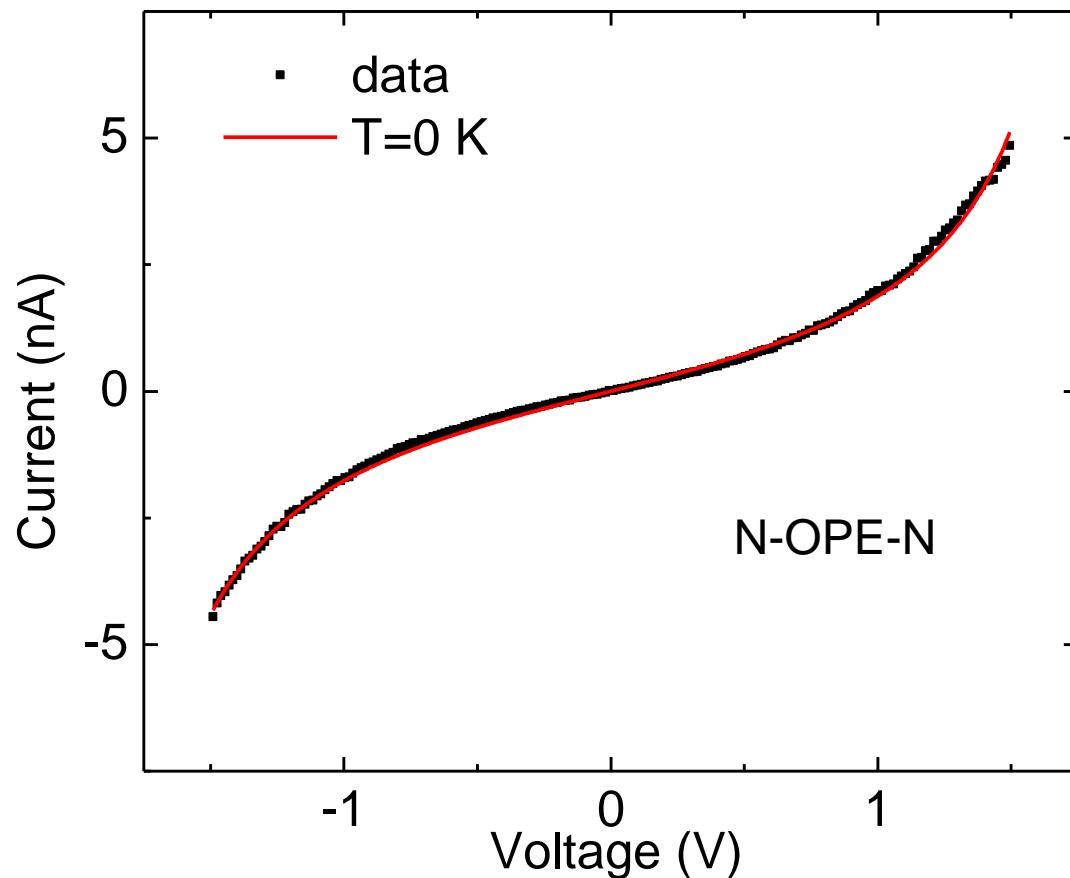
$$I(V) = \frac{8e}{h} \cdot \frac{\Gamma_L\Gamma_R}{\Gamma_L + \Gamma_R} \left[ \arctan \left( \frac{2E_0 + eV \left( \frac{\Gamma_L - \Gamma_R}{\Gamma_L + \Gamma_R} + 1 \right)}{2(\Gamma_L + \Gamma_R)} \right) - \arctan \left( \frac{2E_0 + eV \left( \frac{\Gamma_L - \Gamma_R}{\Gamma_L + \Gamma_R} - 1 \right)}{2(\Gamma_L + \Gamma_R)} \right) \right]$$

3 fit parameters  $\Gamma_1, \Gamma_2, E_0 = E_0(V)$

# one level model: fitting

fitting parameters

$$\Gamma_{\text{low}}, \Gamma_{\text{high}}, E_0$$



# one level model: fitting

fitting parameters

$$\Gamma_{\text{low}}, \Gamma_{\text{high}}, E_0$$

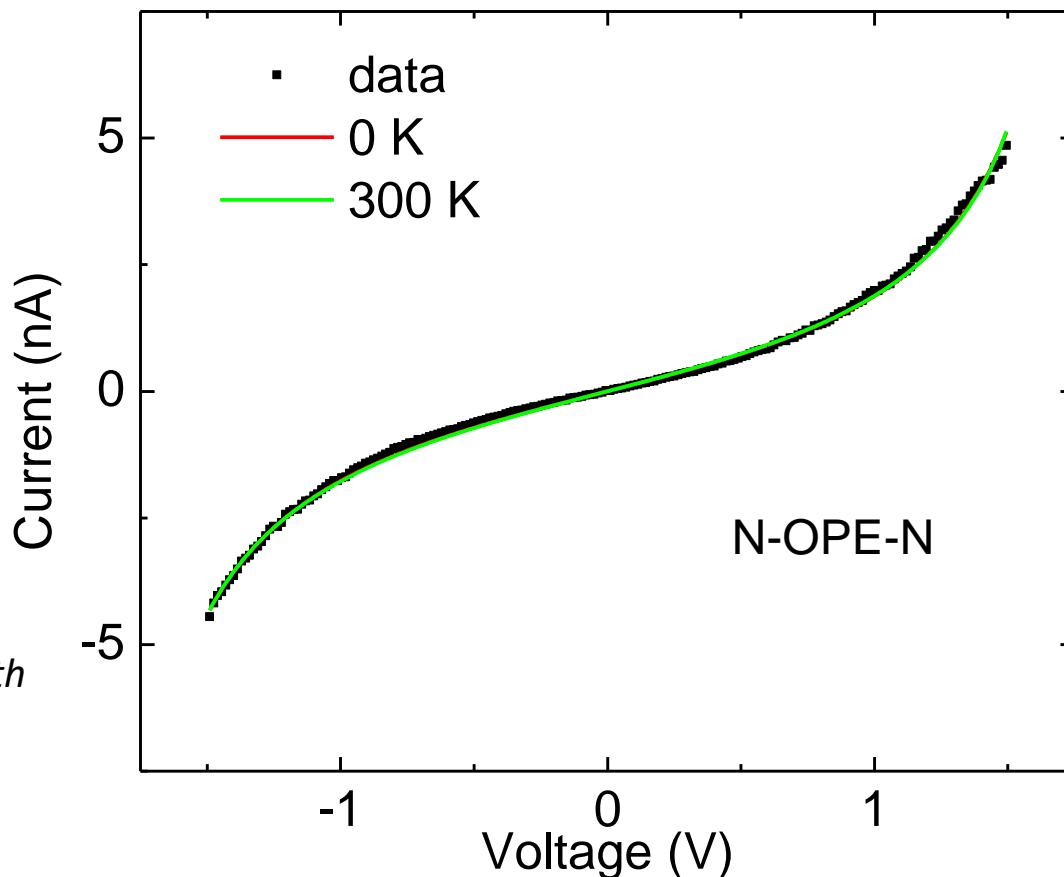
from fit

$$\Gamma_{\text{low}} \approx 2.1 \text{ meV}$$

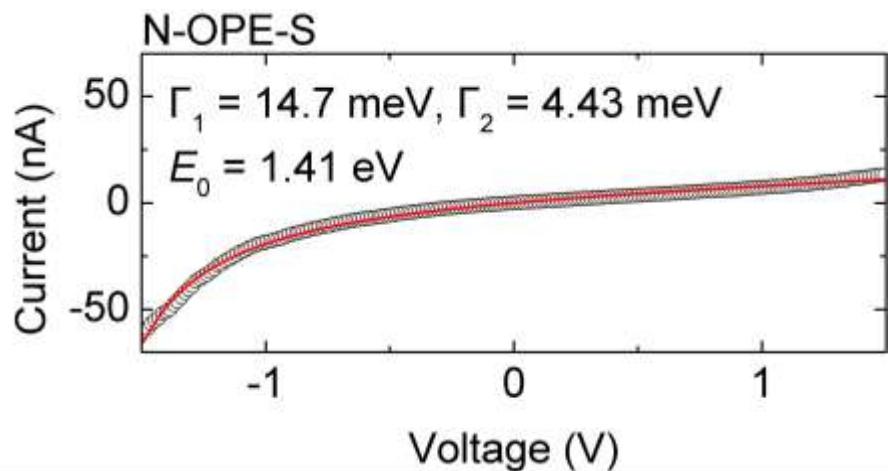
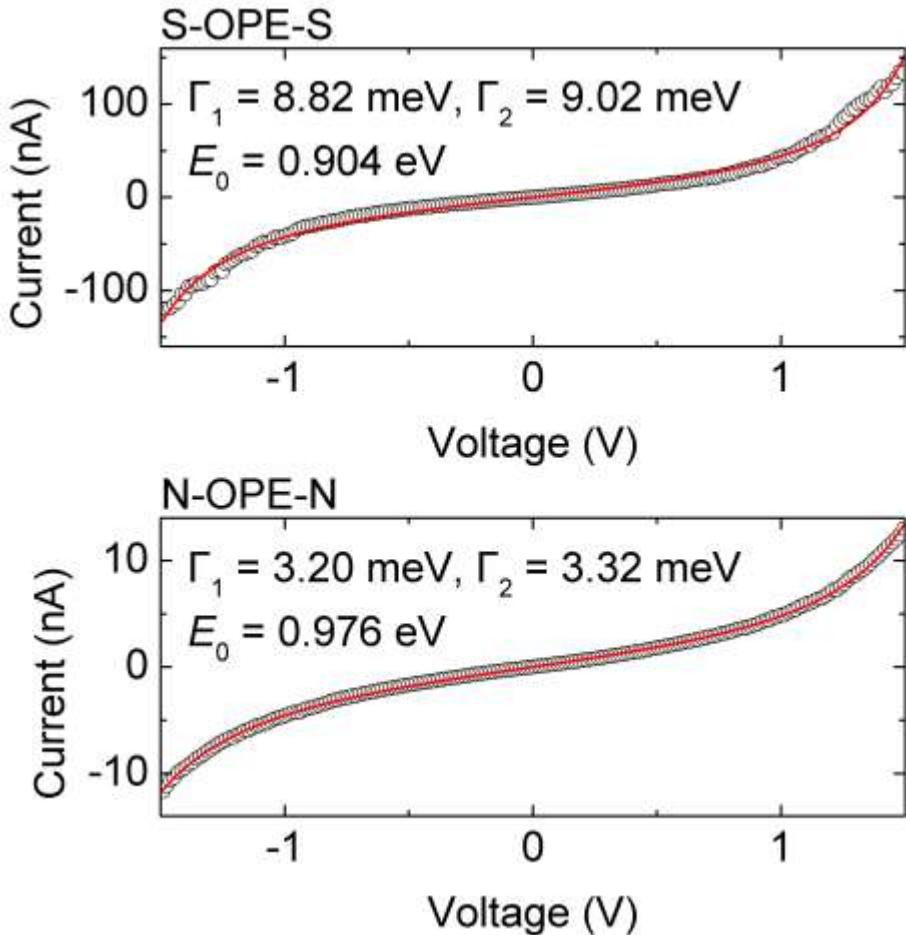
$$\Gamma_{\text{high}} \approx 2.2 \text{ meV}$$

$$E_0 \approx 1.0 \text{ eV}$$

*NB no substantial difference with  
 $T=0$  fit (not at resonance)*



# one level model: fitting avg IV curves



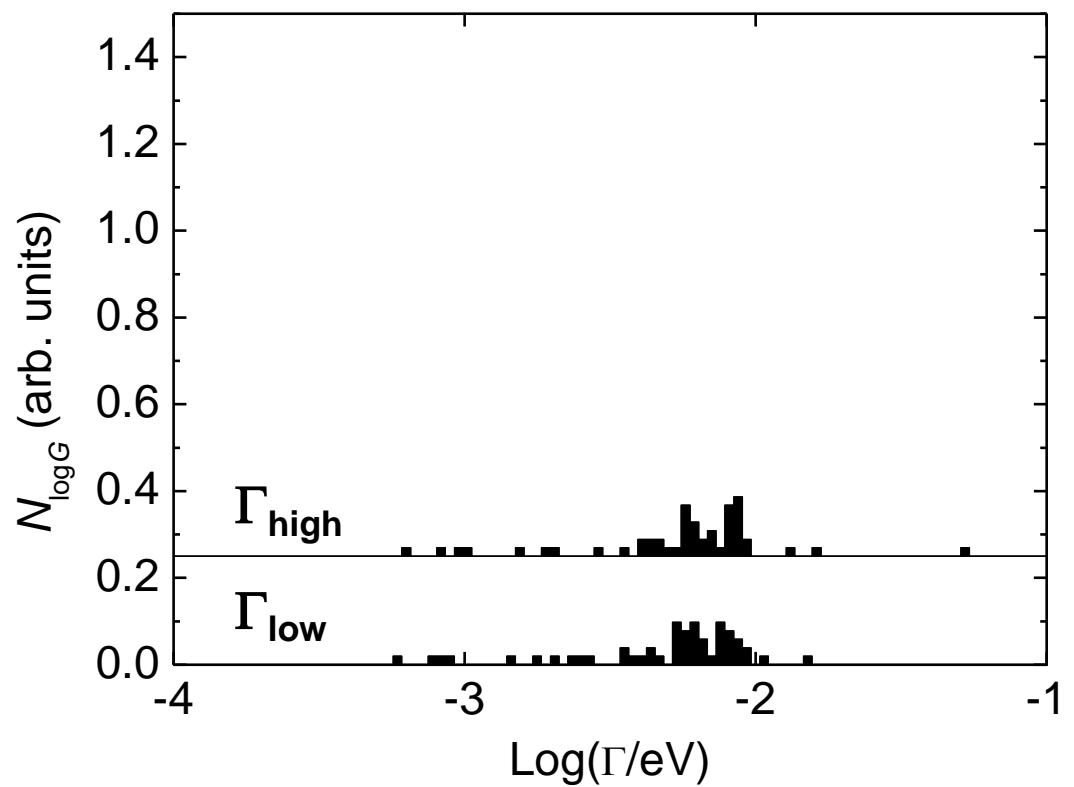
fitting parameters

- $\Gamma_1, \Gamma_2, E_0$
- ⇒ ***symmetry of molecule reflected in symmetry of average IV***
- ⇒ ***coupling is different for N and S***

*NB: no substantial effect of T on fitting (not at resonance)*

# statistics for coupling constants

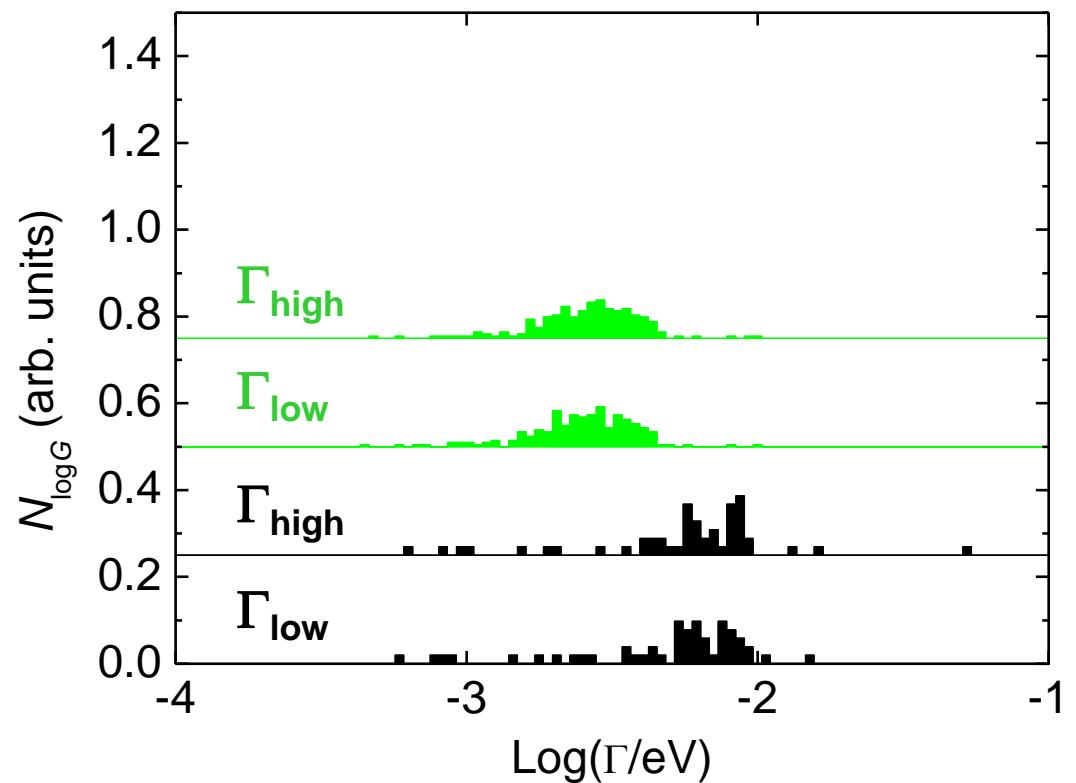
S-OPE-S



# statistics for coupling constants

N-OPE-N

S-OPE-S

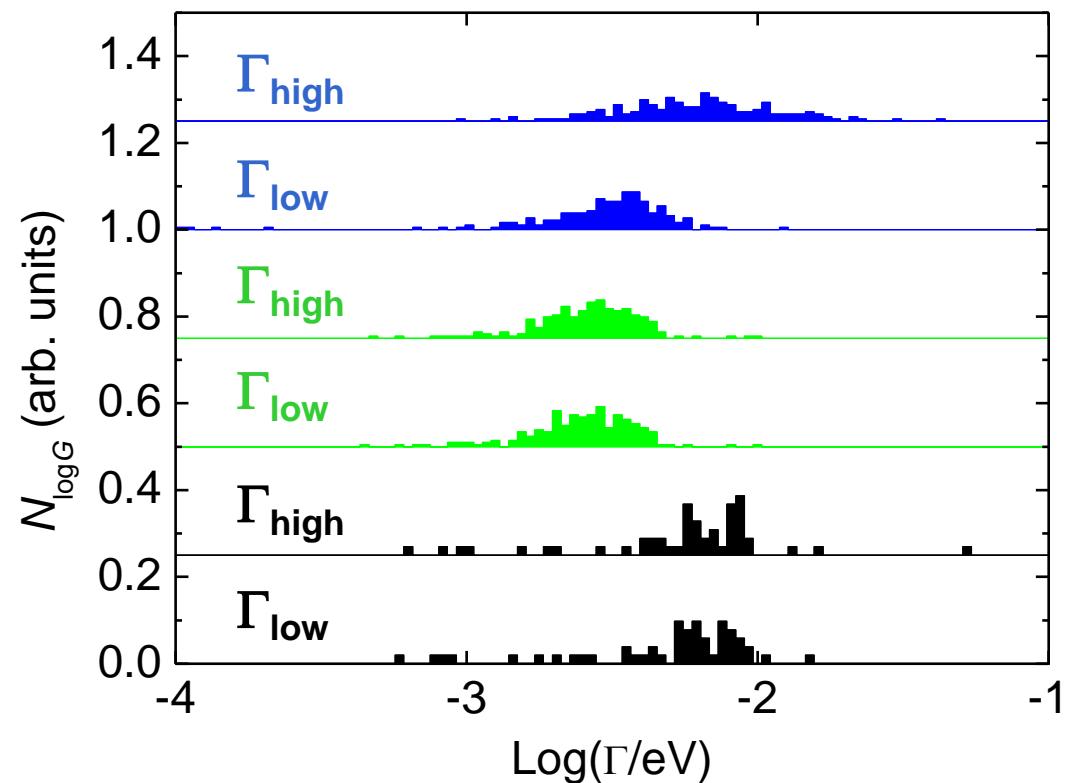


# statistics for coupling constants

N-OPE-S

N-OPE-N

S-OPE-S



# statistics for coupling constants

## plateaus statistics

N-OPE-S: 183

108 asymmetric (60%)

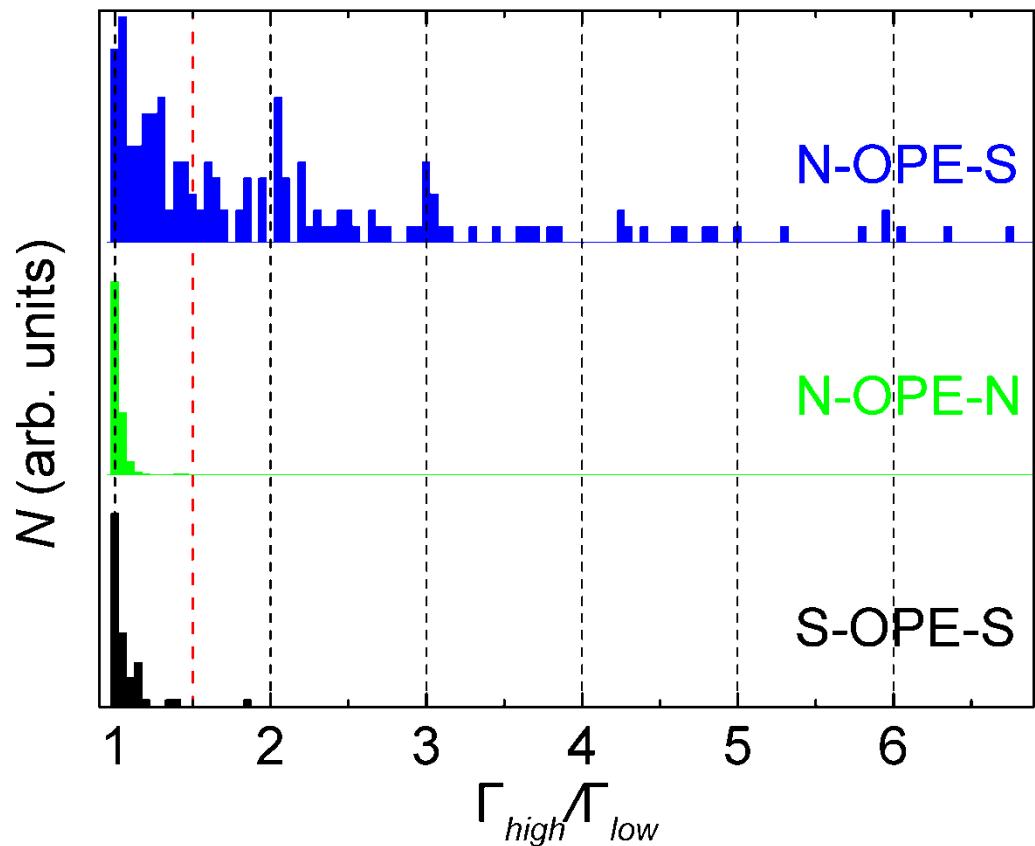
*threshold: 1.5*

N-OPE-N: 205

S-OPE-S: 51

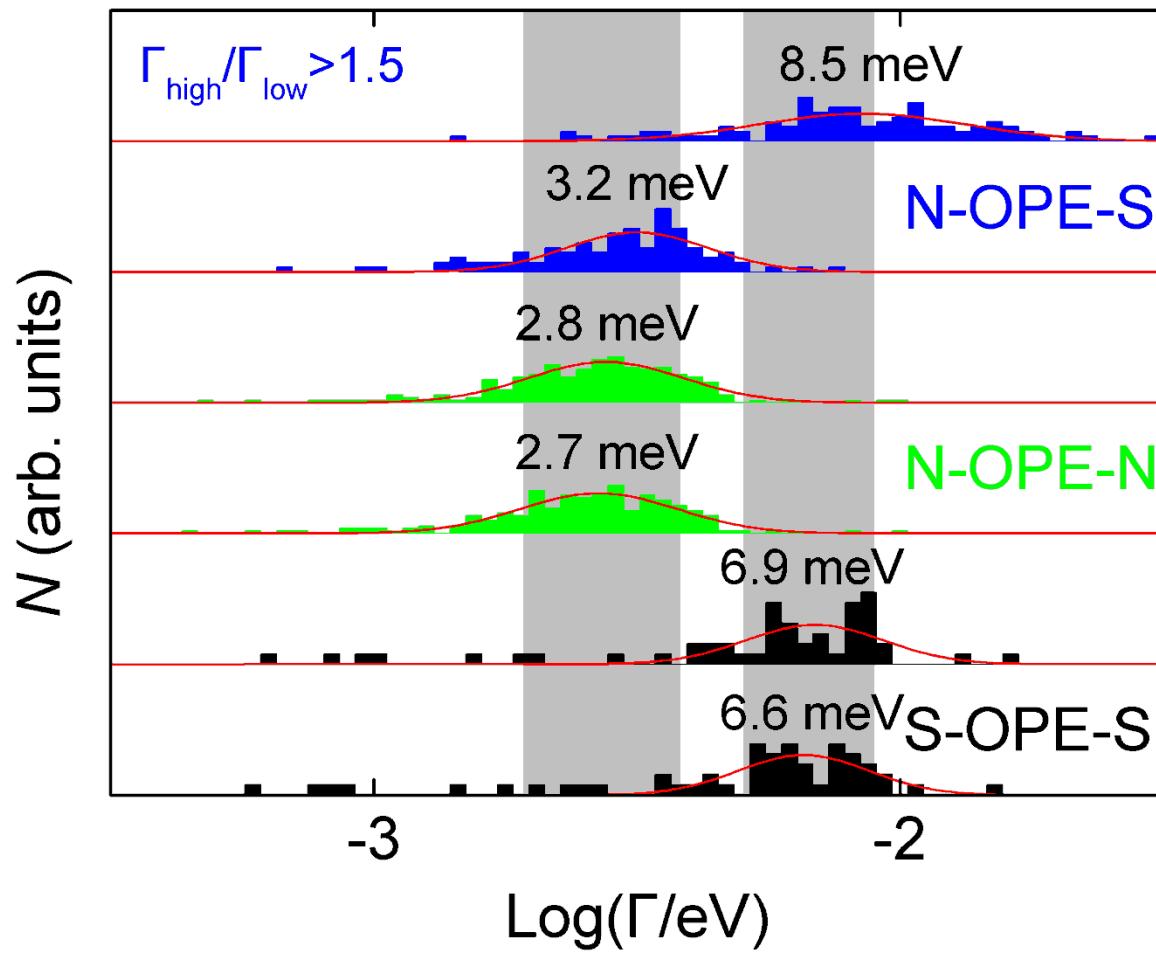
ratio  $\Gamma_{\text{high}} / \Gamma_{\text{low}}$

## asymmetry of IV curves



# statistics for coupling constants

high and low gammas



for recent parameter values for sym and asym molecules, see e.g.:

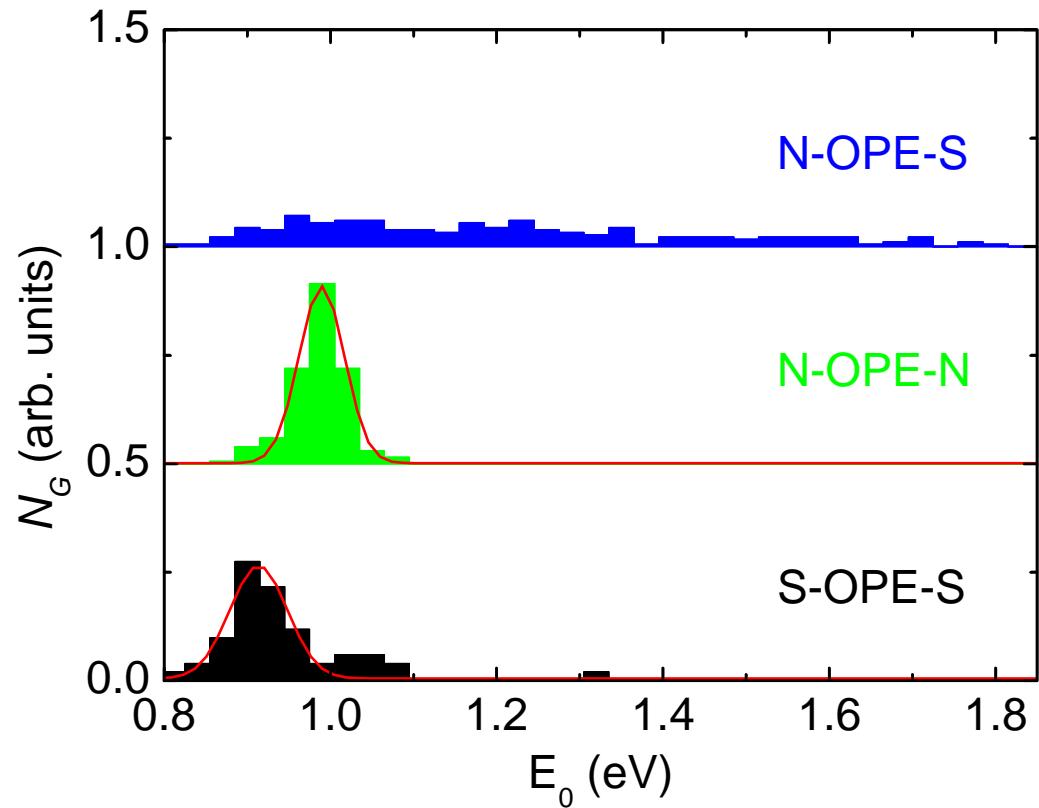
Zotti et al., Small (2010), Kirchner et al., A. Phys. Pol. A (2012), Y.Kim et al., Nano Lett. (2012), Wandlowski et al., JACS (2012)

# statistics for level position

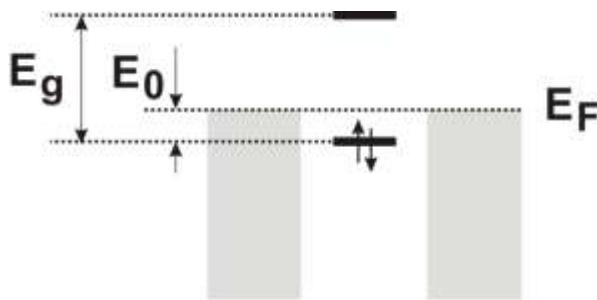
peak values for level position

N-OPE-N:  $E_0 \approx 0.99$  eV  
 $(w \approx 50\text{meV})$

S-OPE-S:  $E_0 \approx 0.91$  eV  
 $(w \approx 70\text{meV})$



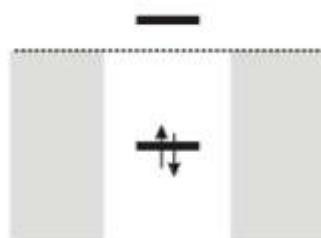
# statistics for level position



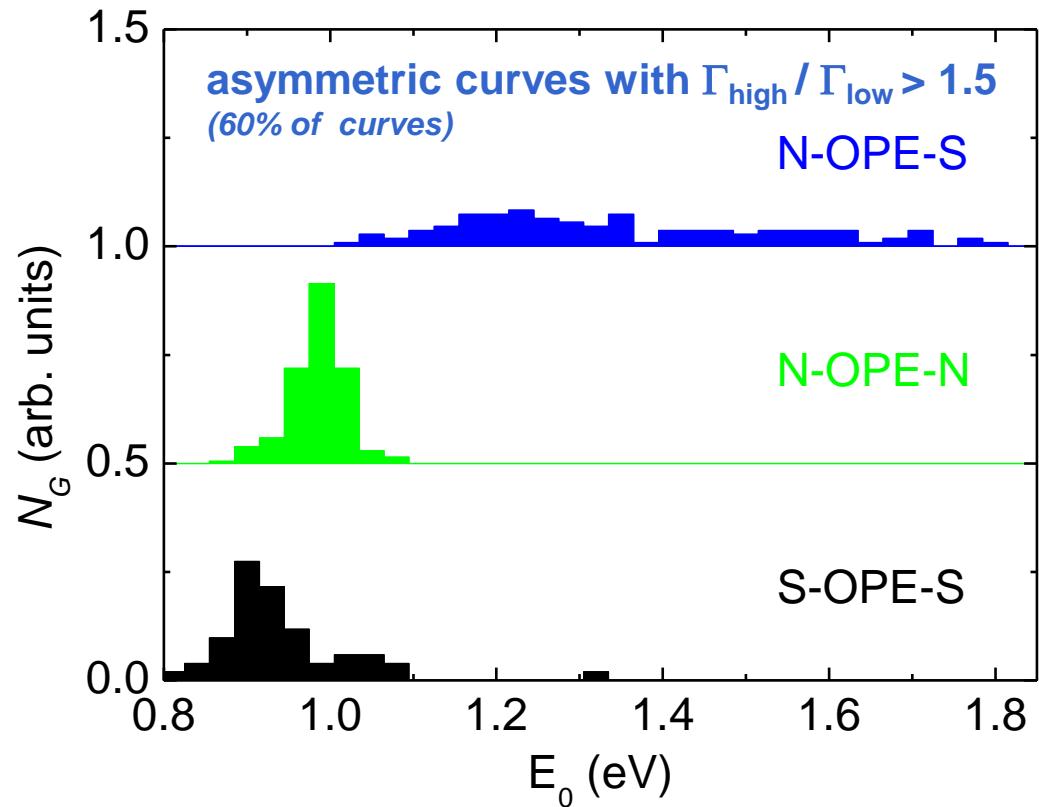
- for N-OPE-S, expect:

$$E_0 \in [E_0^S, E_0^N]$$

- HOMO, LUMO...

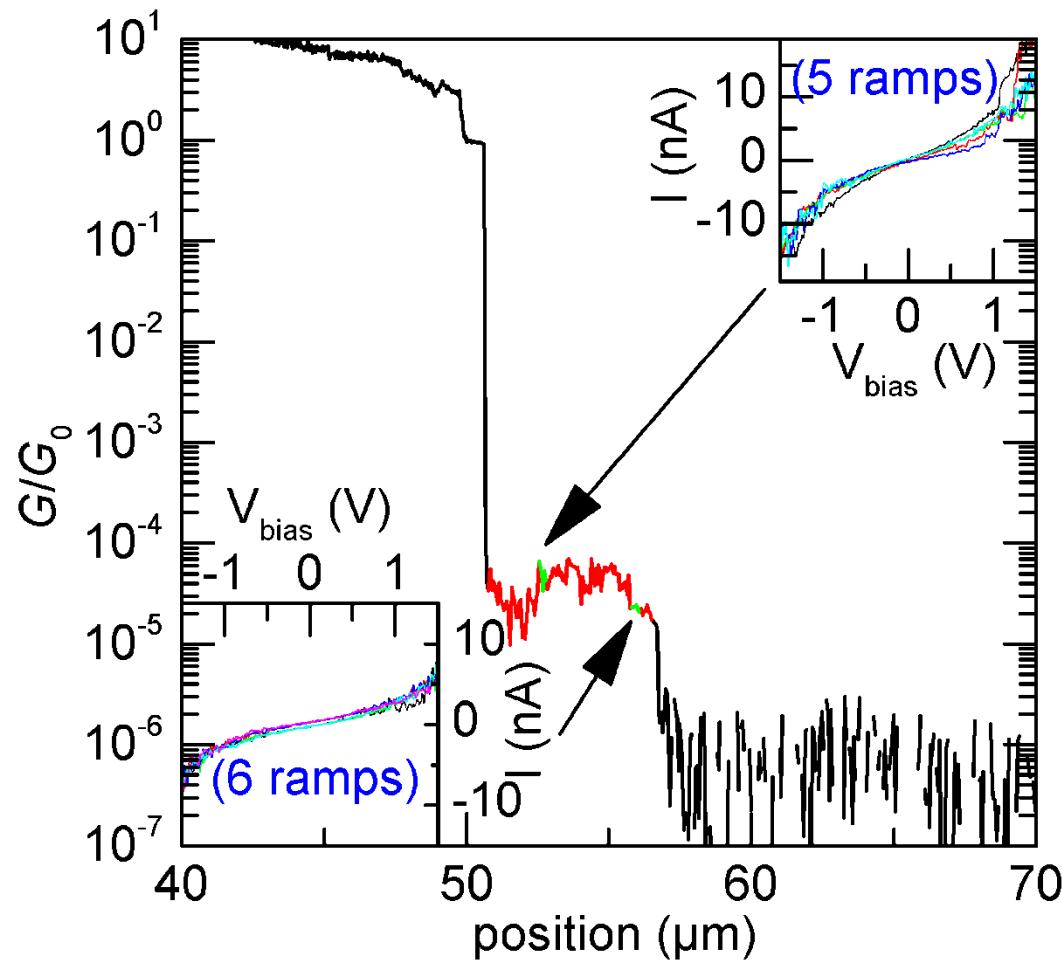
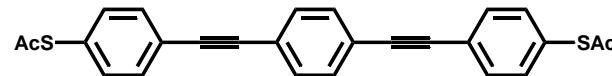


$$\max(E_0) = E_g/2$$

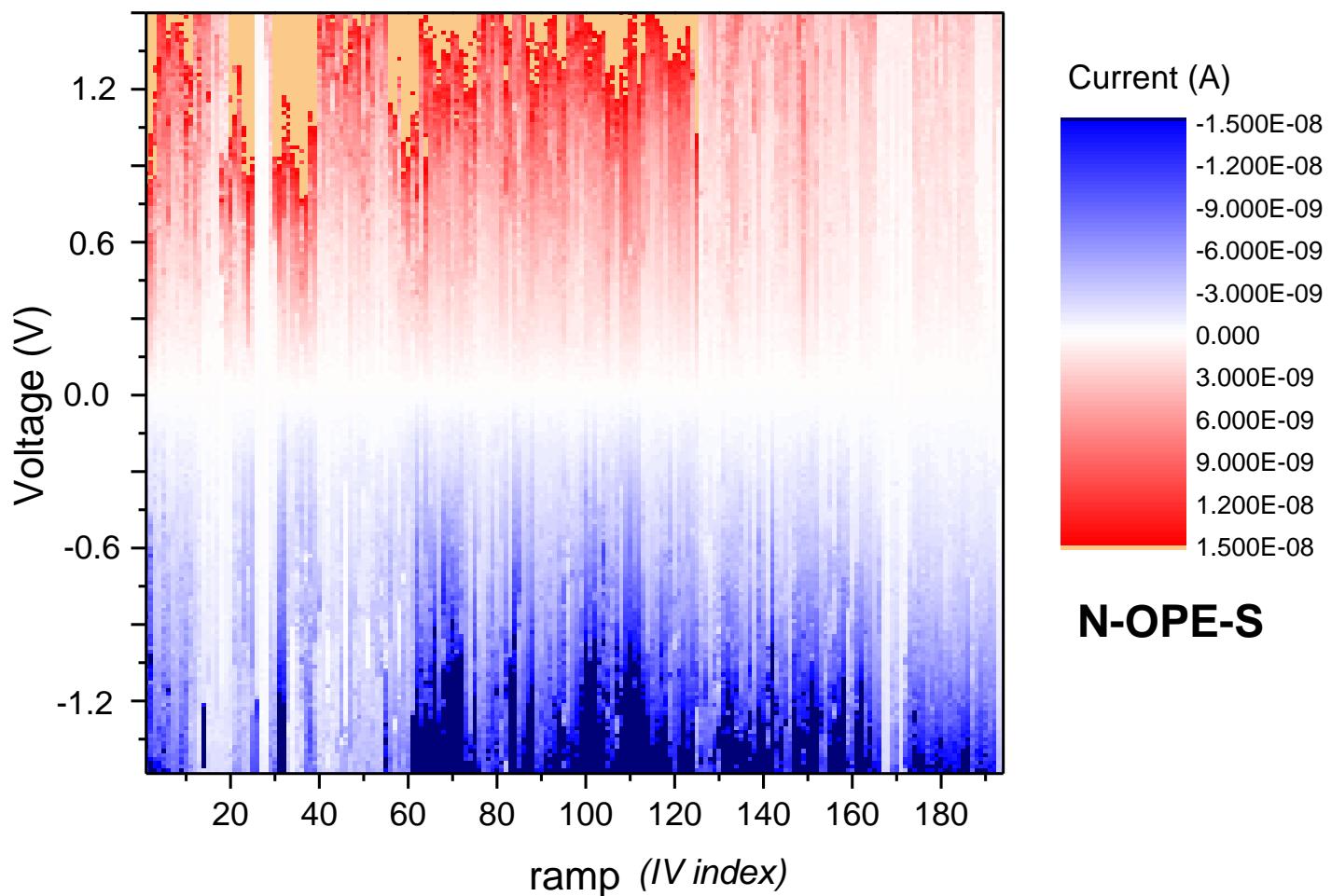


⇒ **HOMO-mediated transport for S-OPE-S**  
**LUMO-mediated transport for N-OPE-N**

# evolution of individual IVs



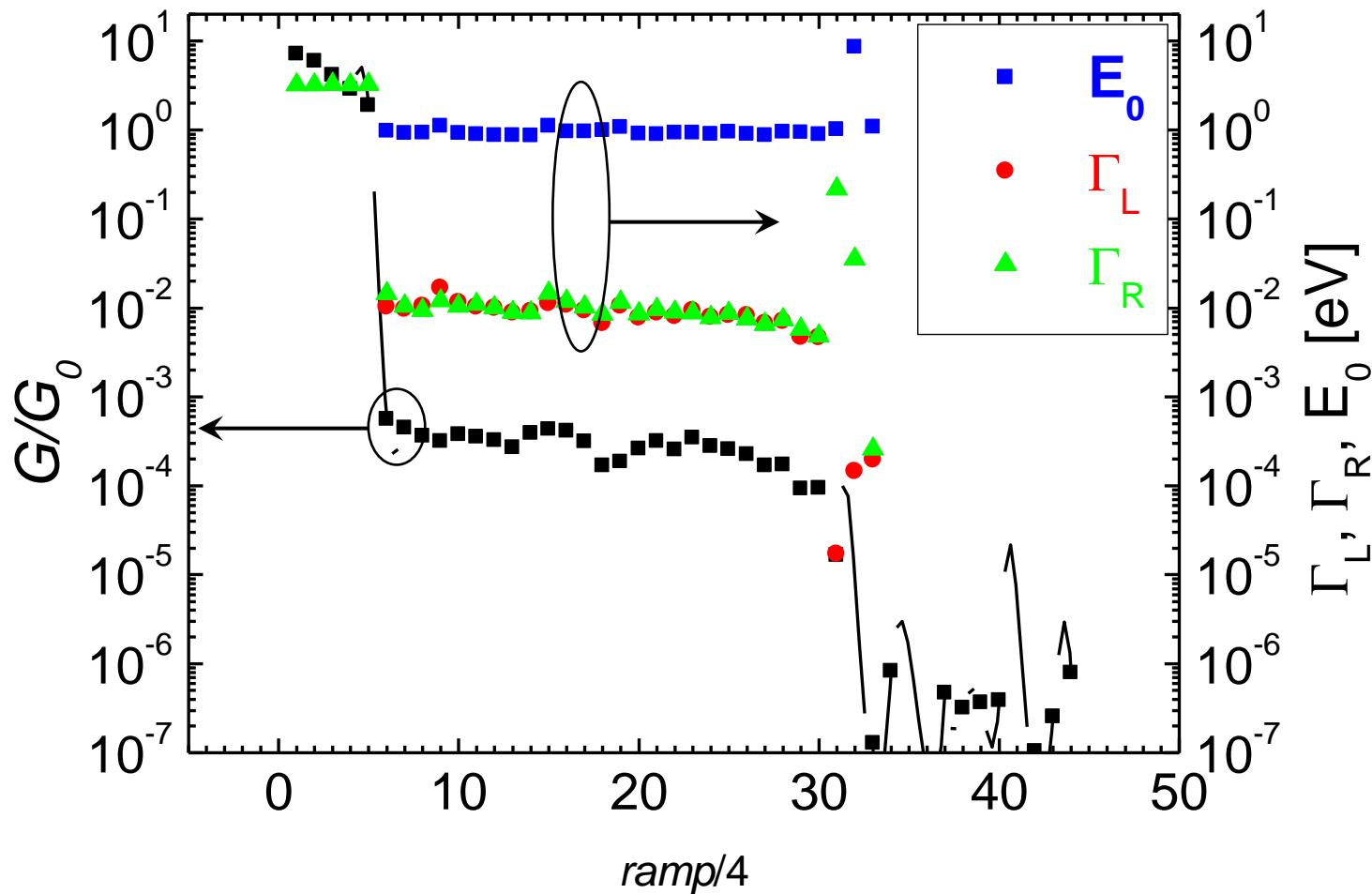
# IVs along a conductance plateau



# evolution of IVs parameters along conductance plateaus

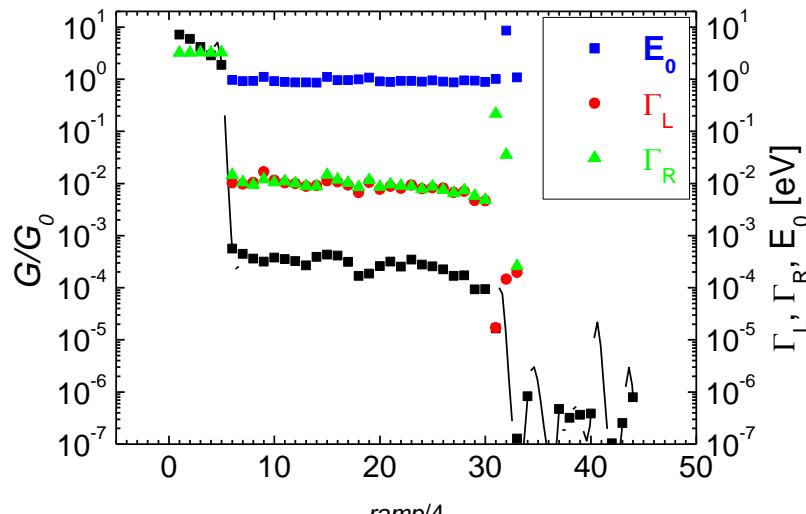
S-OPE-S

*local averaging  
over 4 IVs  
to limit effect of  
"broken" IVs  
(jumps, steps)*

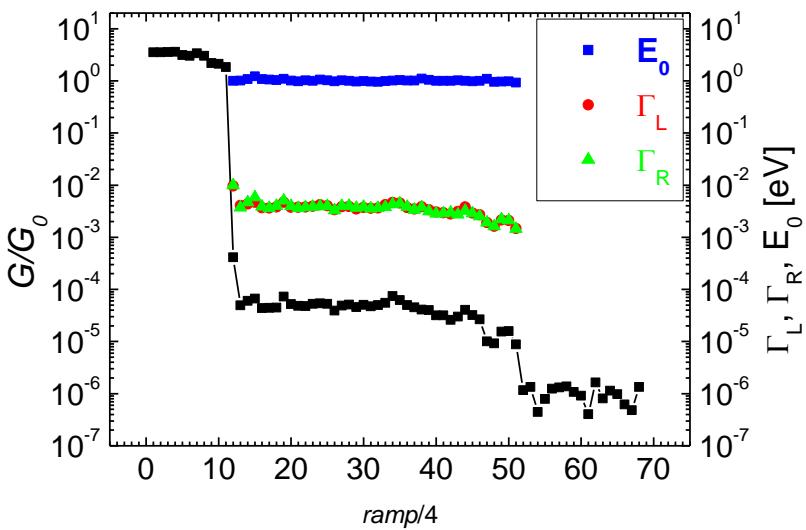


# evolution of IVs parameters along conductance plateaus

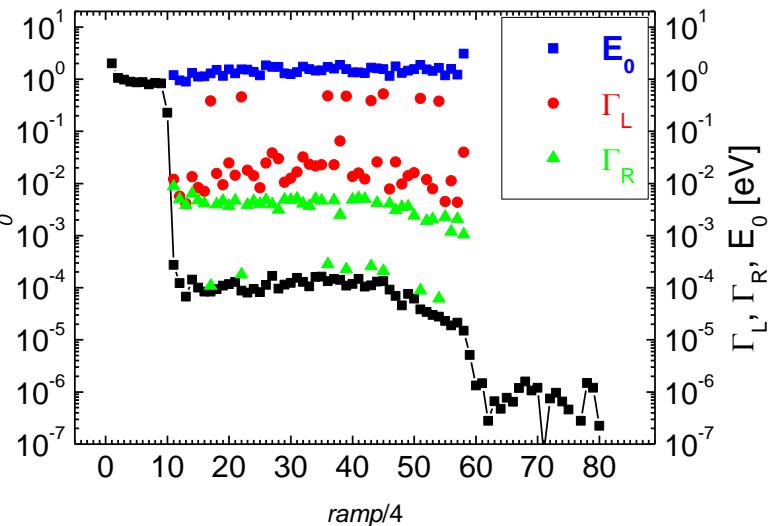
S-OPE-S



N-OPE-N



N-OPE-S



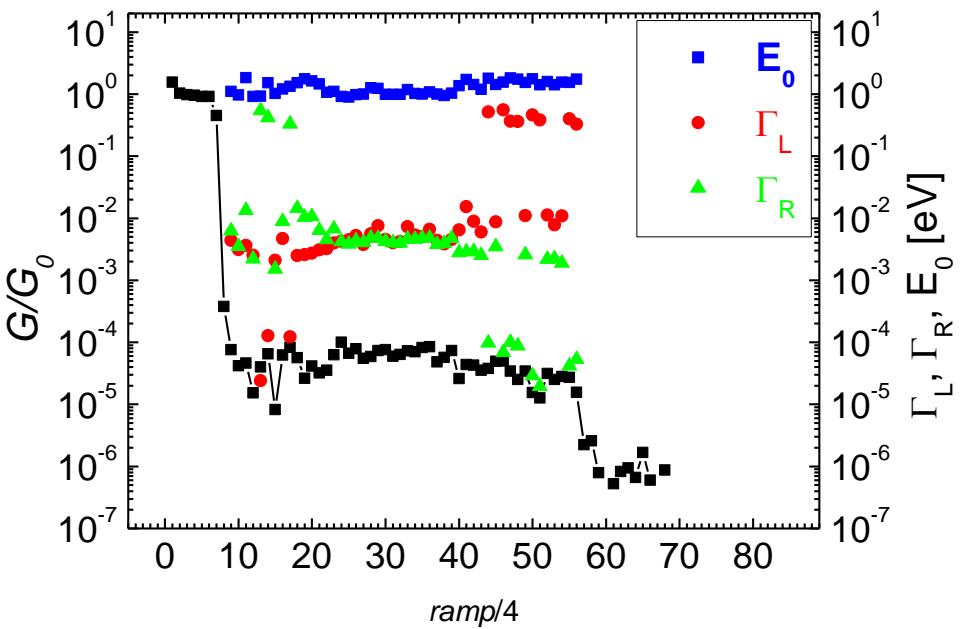
$\Rightarrow$  asymmetric IVs during most of plateau length for N-OPE-S

NB: fits to locally averaged IVs (4) to limit effect of "broken" IVs (jumps, steps)

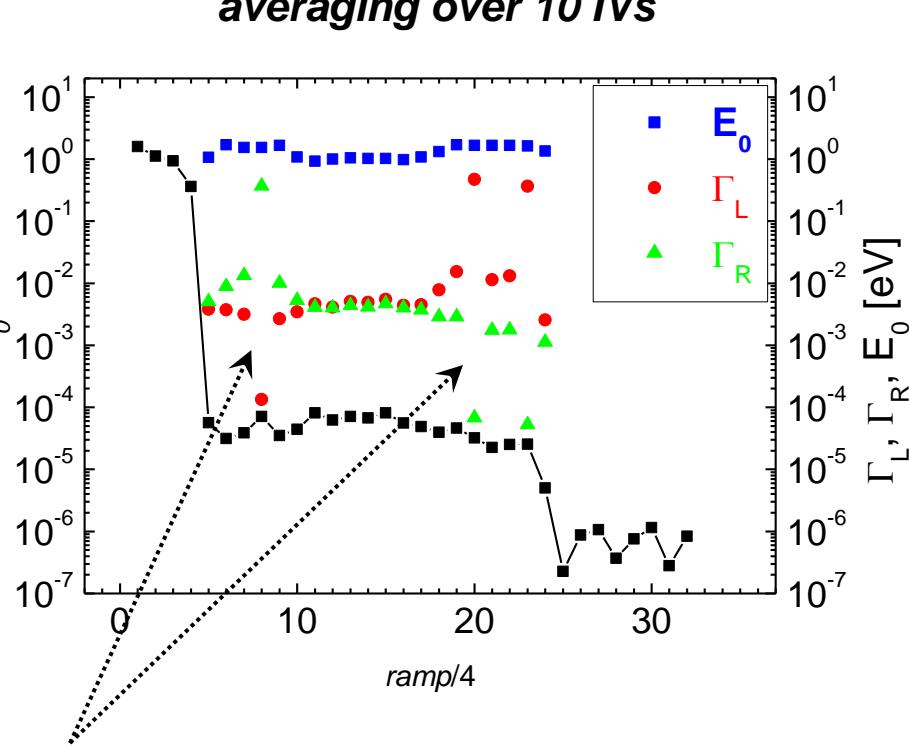
# asymmetric molecule: a particular case

**avg. IV ~ symmetric but individual IVs are not all symmetric**

N-OPE-S



averaging over 10 IVs

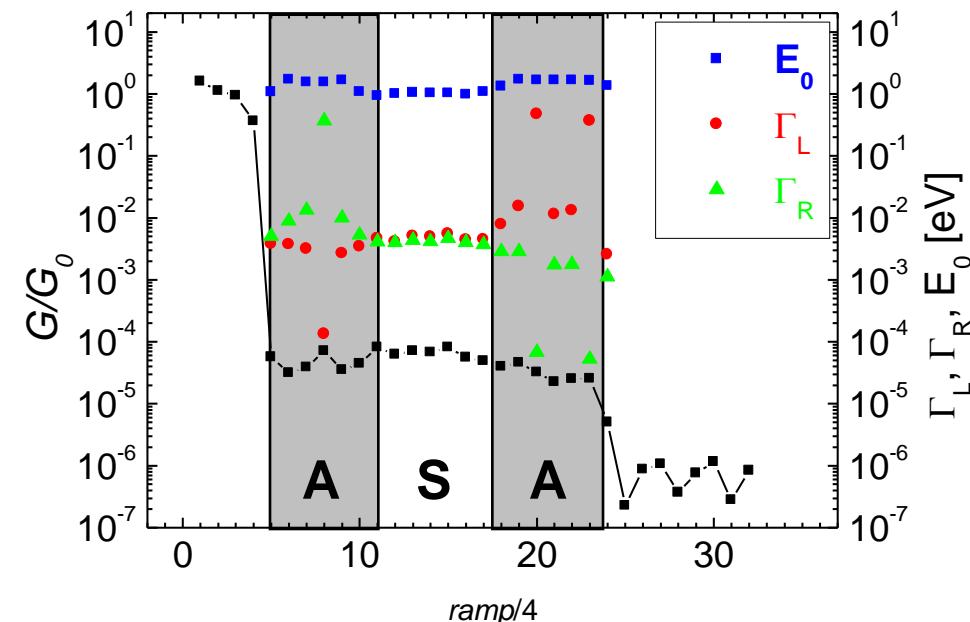
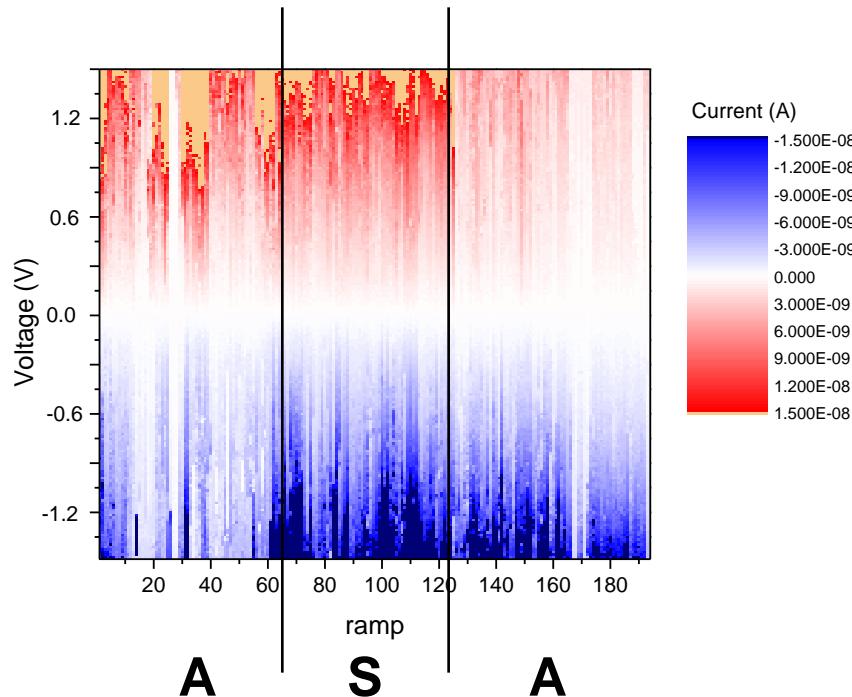


***inversion of IV curve asymmetry***

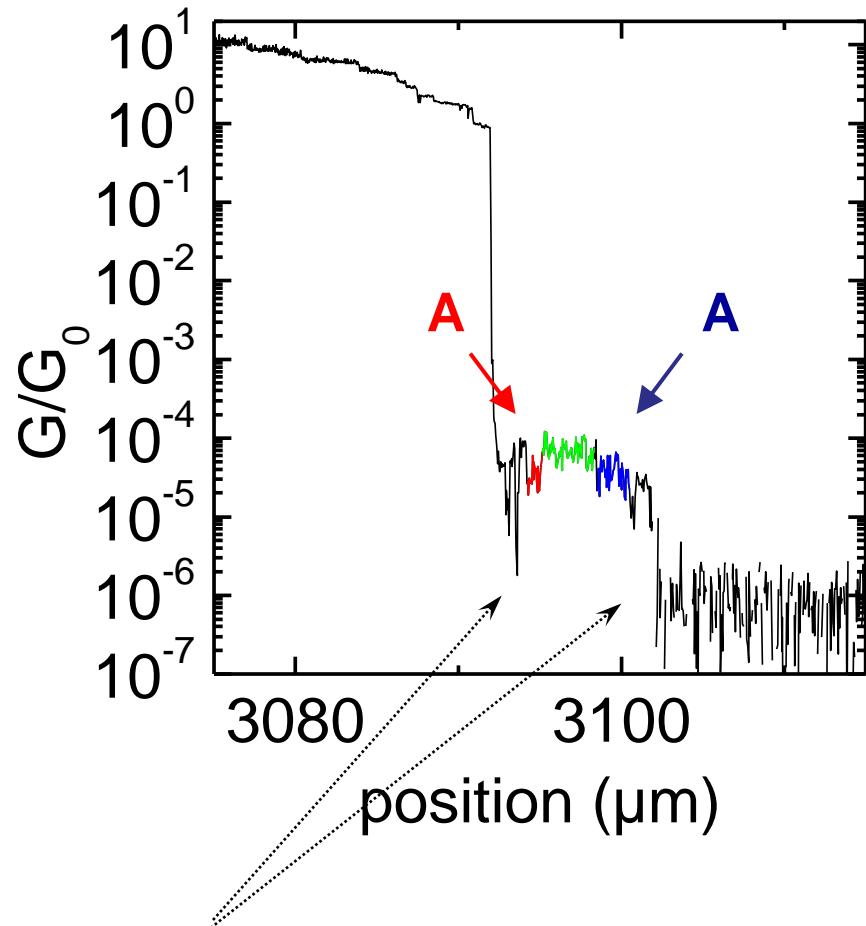
# asymmetric molecule

N-OPE-S

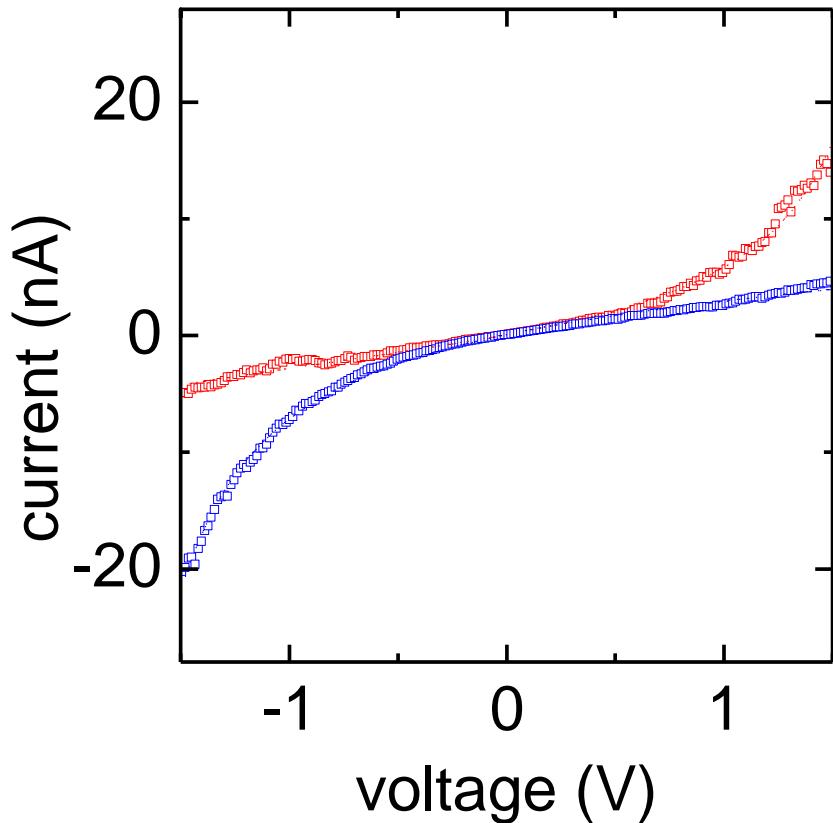
*averaging over 10 IVs*



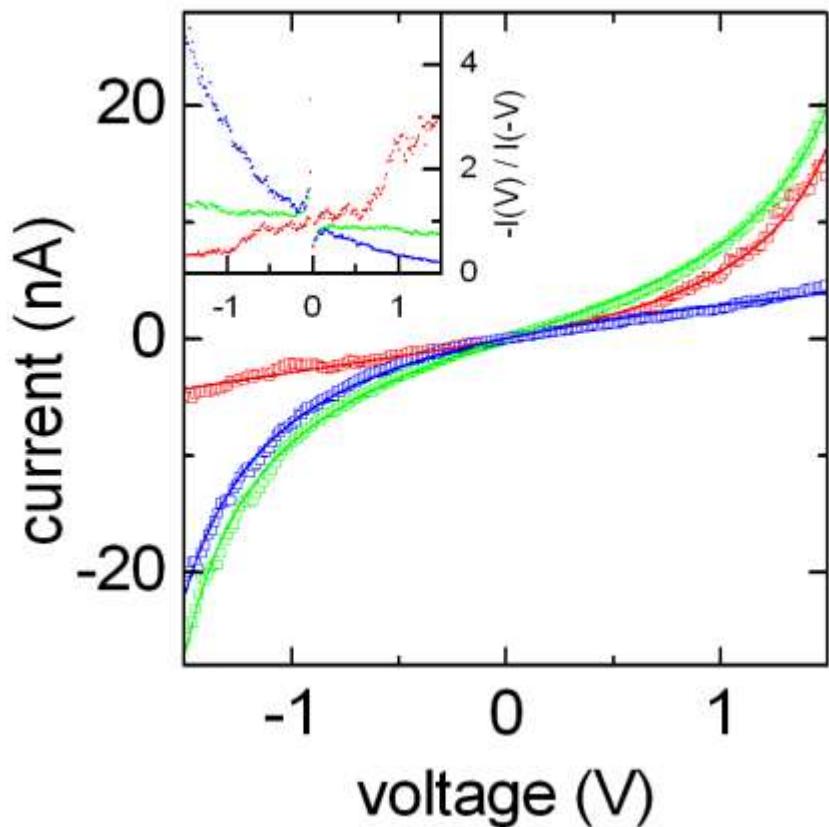
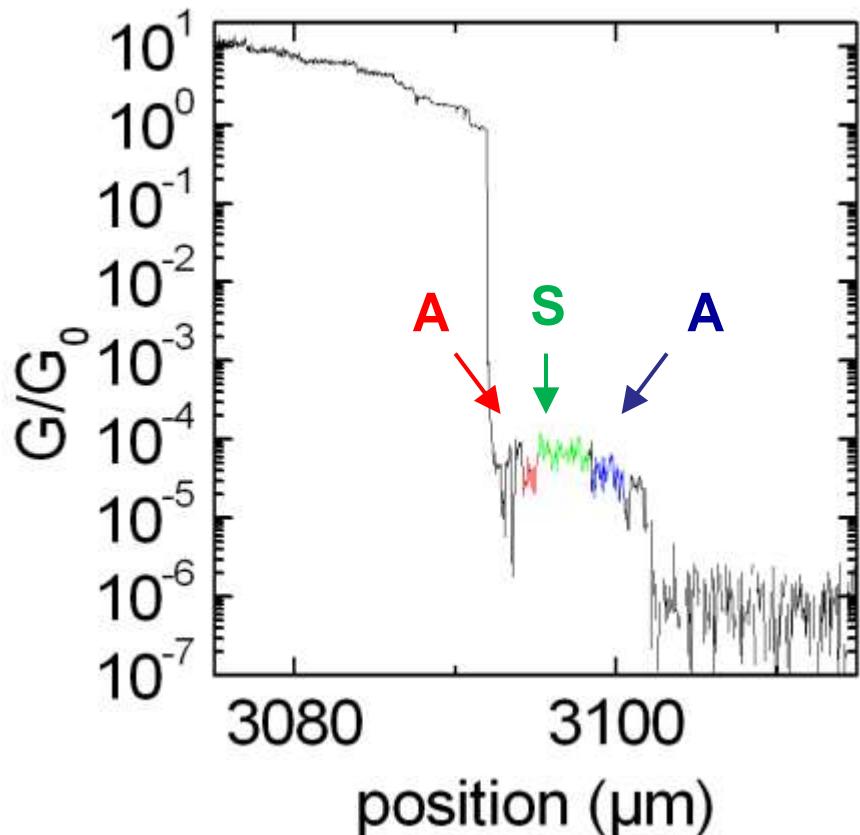
# asymmetric molecule



***exclude very noisy  
("dynamic") region***



# asymmetric molecule



$$E_0 \approx 1.4 \text{ eV}$$

$$\Gamma_L \approx 3.0 \text{ meV}$$

$$\Gamma_R \approx 7.0 \text{ meV}$$

$$E_0 \approx 0.97 \text{ eV}$$

$$\Gamma_L \approx 4.6 \text{ meV}$$

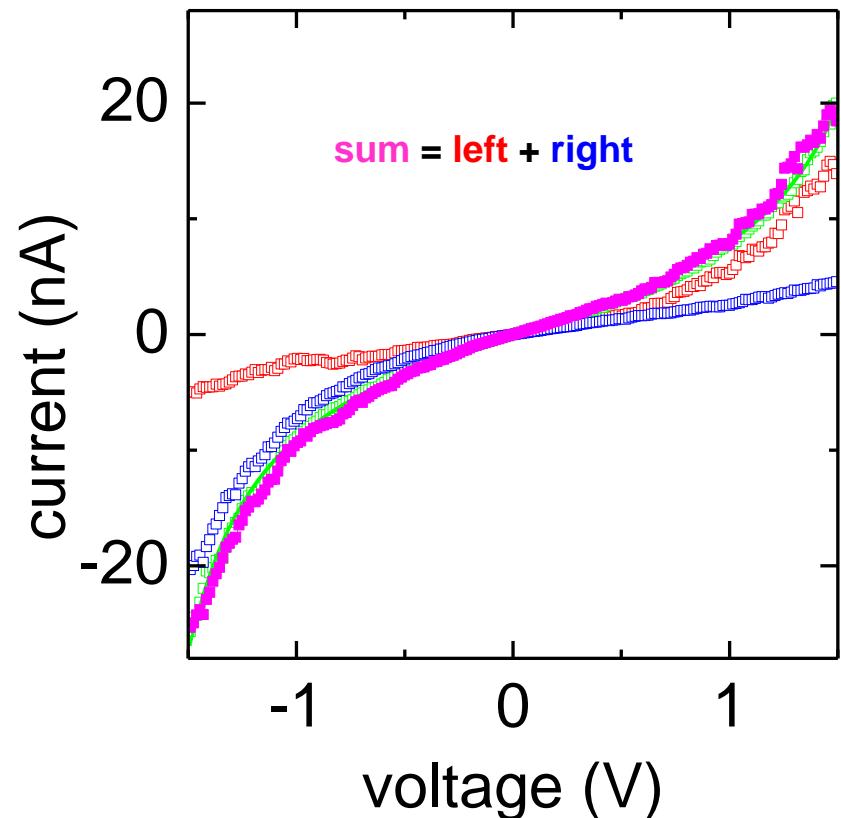
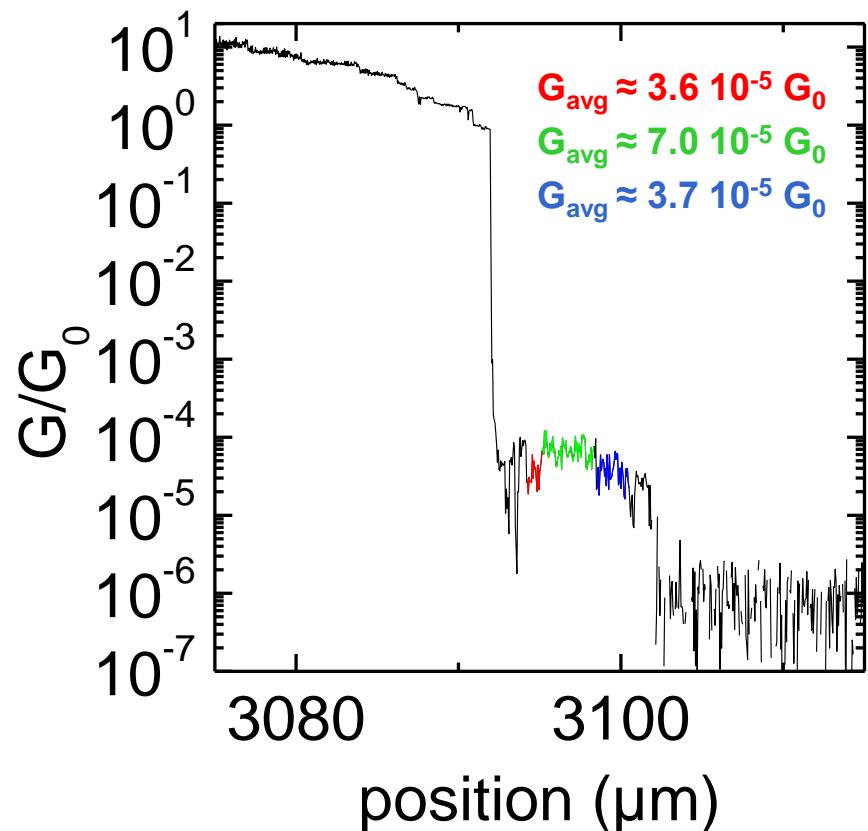
$$\Gamma_R \approx 4.2 \text{ meV}$$

$$E_0 \approx 1.6 \text{ eV}$$

$$\Gamma_L \approx 12.9 \text{ meV}$$

$$\Gamma_R \approx 2.6 \text{ meV}$$

# asymmetric molecule



$$E_0 \approx 1.4 \text{ eV}$$

$$\Gamma_L \approx 3.0 \text{ meV}$$

$$\Gamma_R \approx 7.0 \text{ meV}$$

$$E_0 \approx 0.97 \text{ eV}$$

$$\Gamma_L \approx 4.6 \text{ meV}$$

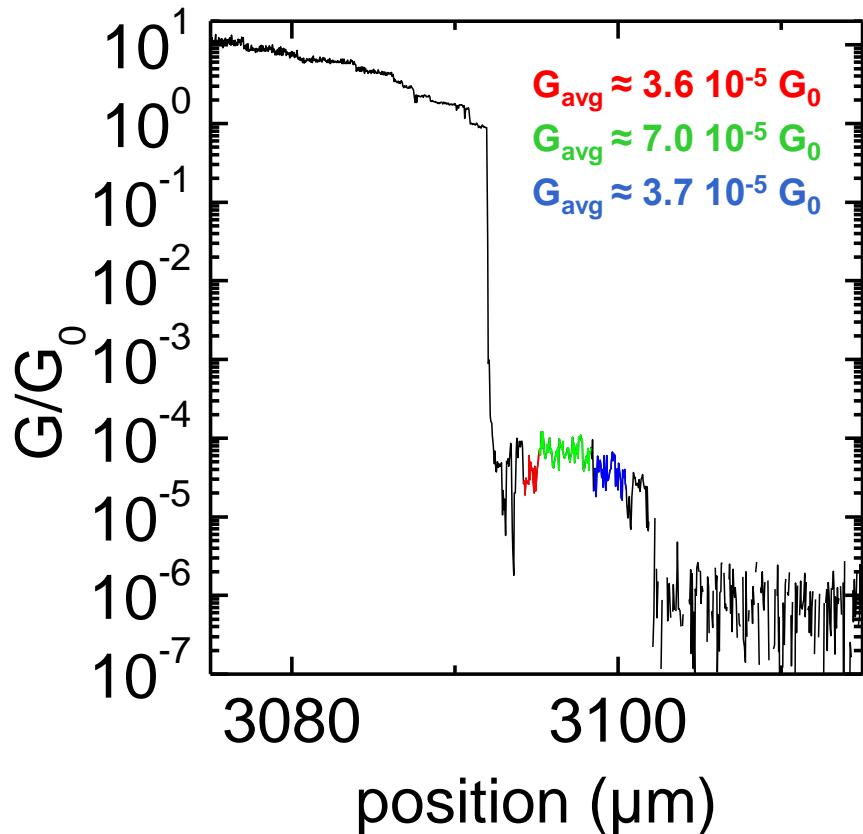
$$\Gamma_R \approx 4.2 \text{ meV}$$

$$E_0 \approx 1.6 \text{ eV}$$

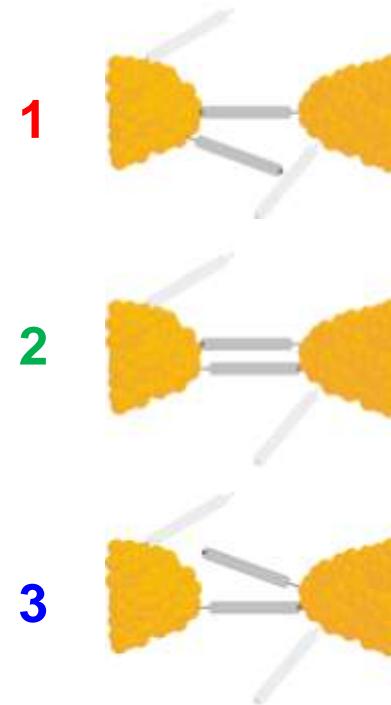
$$\Gamma_L \approx 12.9 \text{ meV}$$

$$\Gamma_R \approx 2.6 \text{ meV}$$

# asymmetric molecule



multiple  
bridging (?)  
(cf  $G$  values)



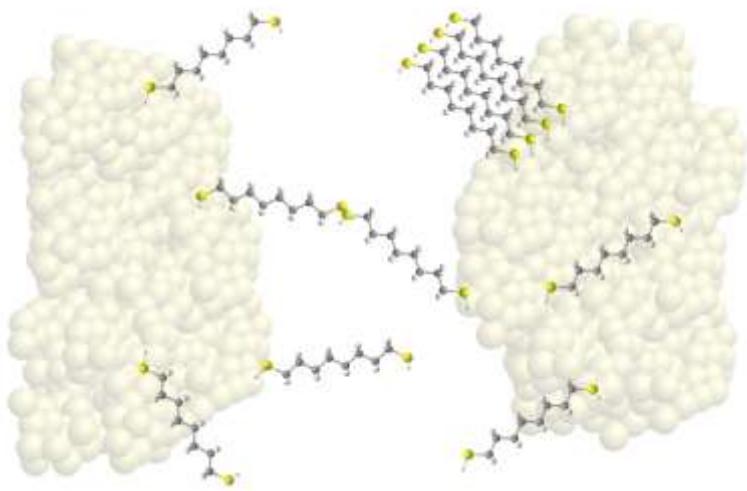
**NB: interference effects** due to multiple pathways: no such observation here

**NB: 2-level model** (e.g. 2 orbitals or 2 mol. with 1 dominant level): no consistent fitting

**NB:** other possible explanations:  $\Gamma, E_0 \neq \text{const.}$  during stretching, interplay between coupling and level position (cf e.g.: "bowl"-shaped plateaus, BDT: Tao et al., Nat. Nano 2012); effect of image charges/screening, partial charge transfer electrode – molecule

# outlook

# outlook: molecular junction formation



*drifting molecules,  
stochastic anchoring,  
random clustering* ⇒ *undefined junction  
geometry &  
conductance*

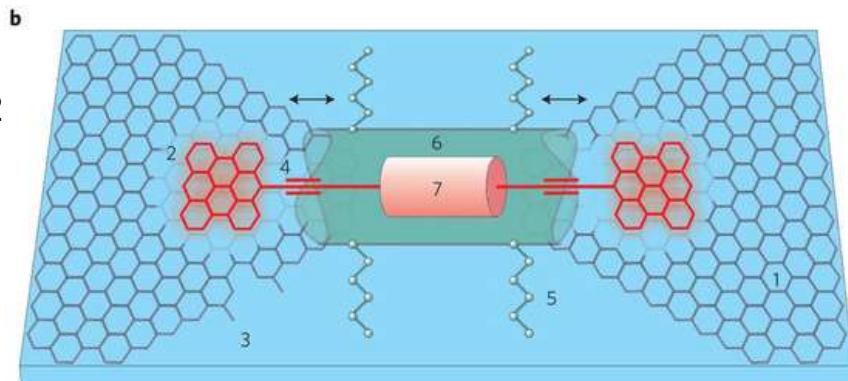
*drifting surface  
atoms, metal  
protrusions* ⇒ *undefined  
electrostatic  
landscape*

⇒ **variability, low-yield and lack of  
control in key electrical parameters**

## Carbon-based contact materials as electrodes

FLG	vd Zandt et al., Nano Lett. 2011
SWNT	Krupke et al., Nat. Nanotech. 2010
C-fiber tips	Agrait et al., Nanoscale Res. Lett. 2012

- ⇒ **monolayer graphene ... ?**
- ⇒ **paradigm shift for  
molecular electronics**



Lötscher, Nat. Nano 2013